Anomaly Detection in Time Series

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I. Introduction

What is a time series? What is an anomaly?

Introduction: Time series are Everywhere

Energy Production



Edf.fr: tinyurl.com/yc7x5xje

Astrophysics



Virgo: https://www.virgo-gw.eu/

Medicine



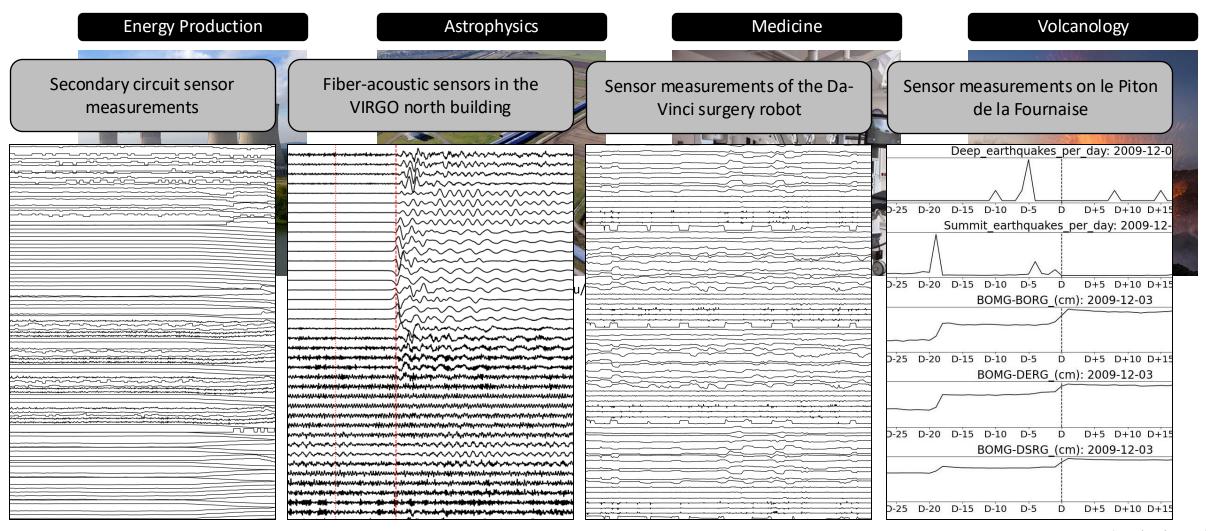
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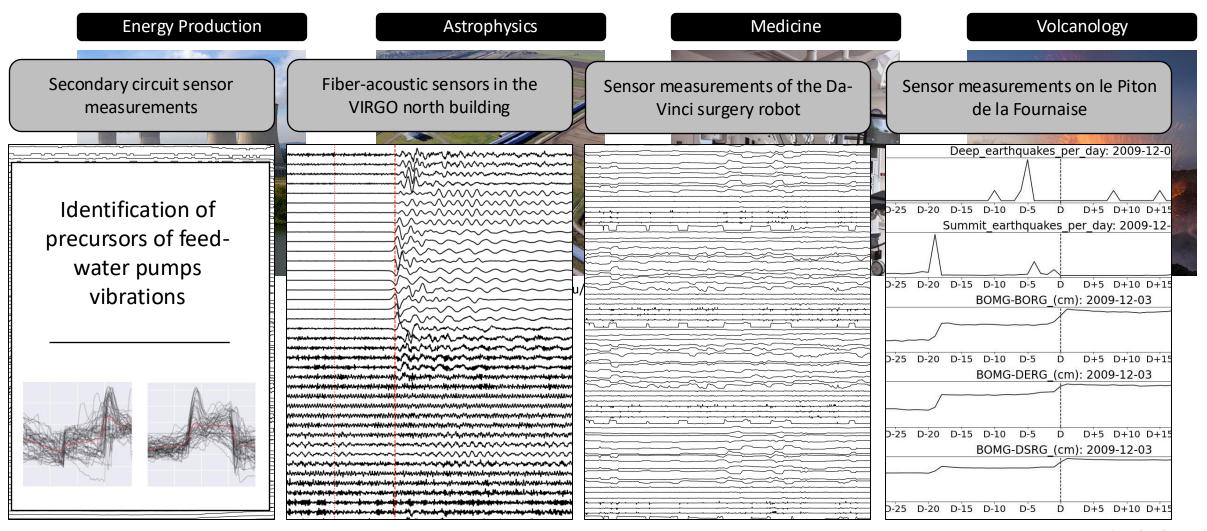
Volcanology

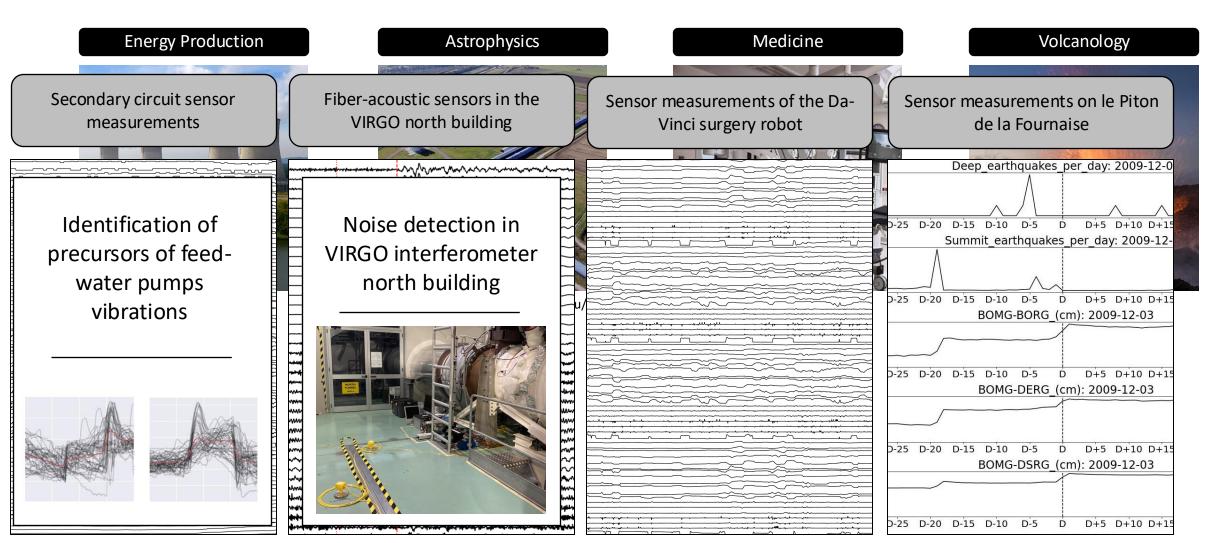


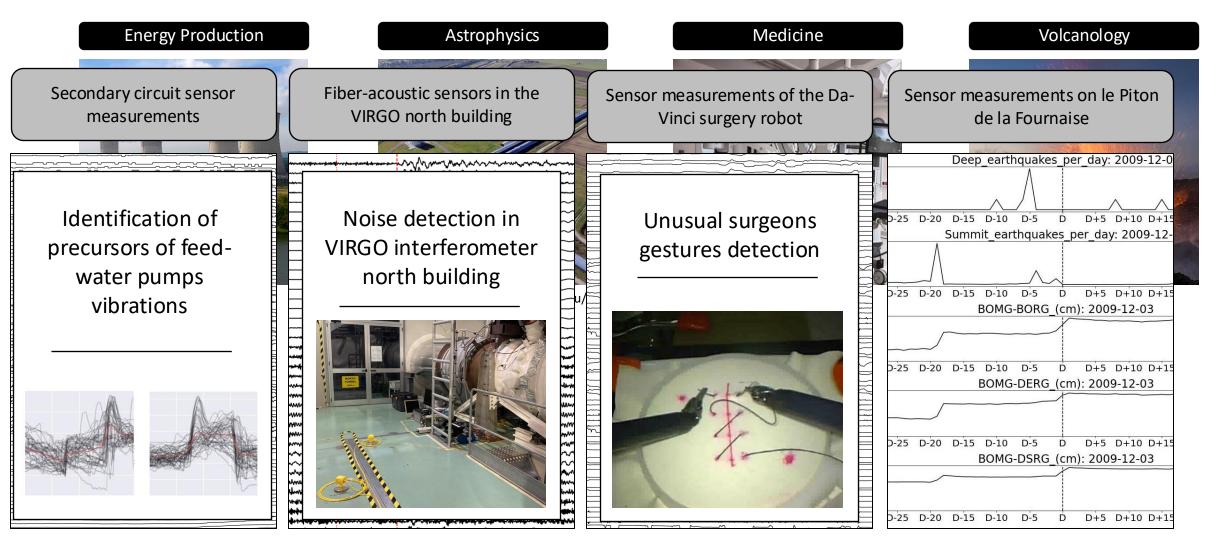
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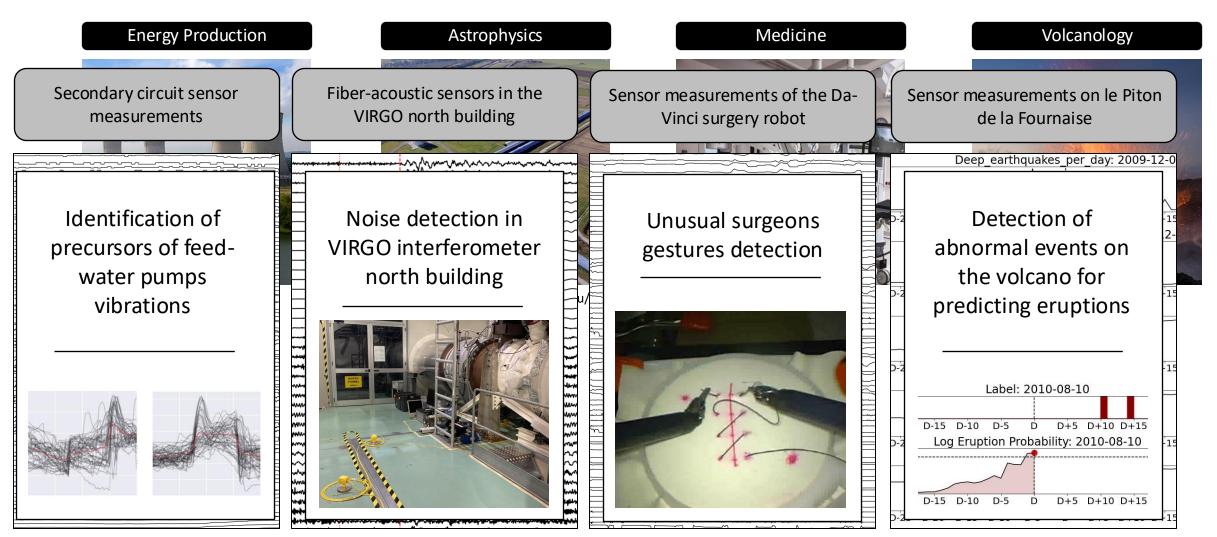
Introduction: Time series are Everywhere









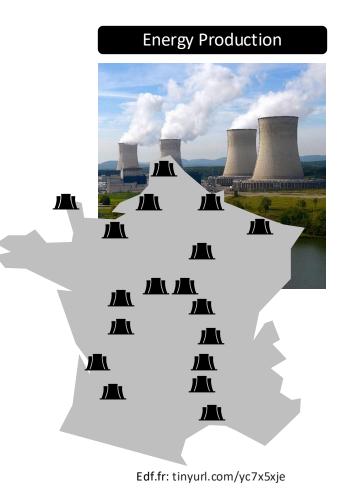


Large-scale time series database

Energy Production



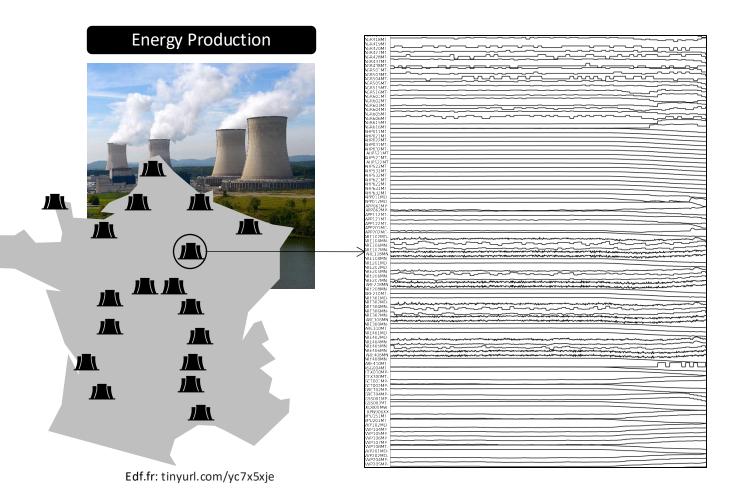
Large-scale time series database



Example of Nuclear production

58 nuclear power plants across France

Large-scale time series database

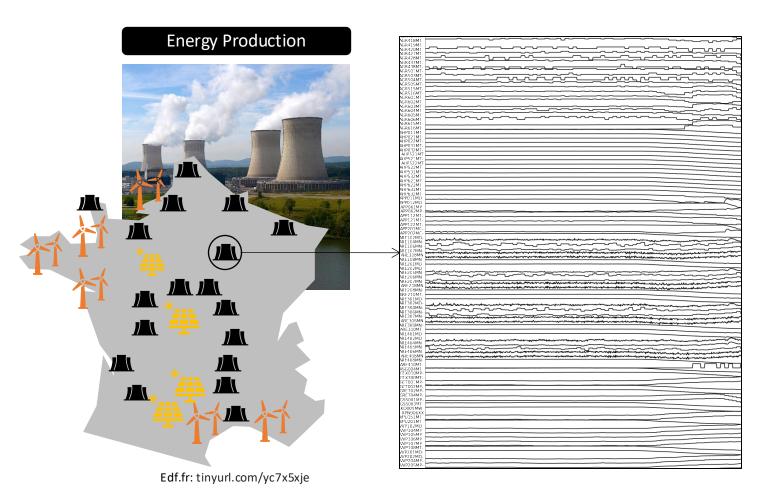


Example of Nuclear production

- 58 nuclear power plants across France
- 2000+ sensors per power plant
- 30 years of data collections

A total of 1.5 PetaBytes

Large-scale time series database



Example of Nuclear production

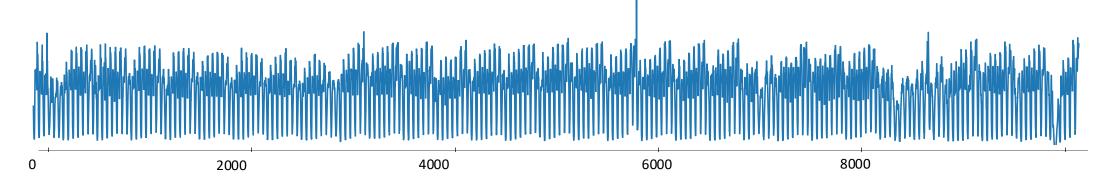
- 58 nuclear power plants across France
- 2000+ sensors per power plant
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A total of 1.5 PetaBytes

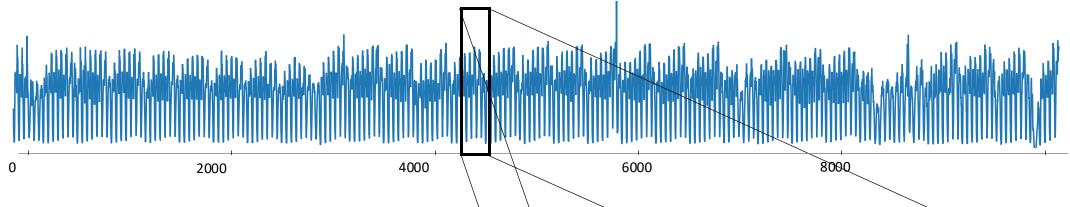
Other source of production

- New sensors with higher acquisition rate

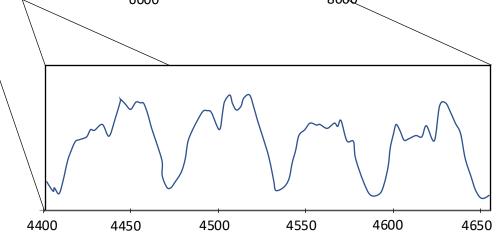
• Time series T (example : number of taxi passengers in New York City)



• Time series T (example : number of taxi passengers in New York City)



• Subsequence $T_{i,\ell}$ with $i=4400,\ell=250$



• Time series T (example : number of taxi passengers in New York City)

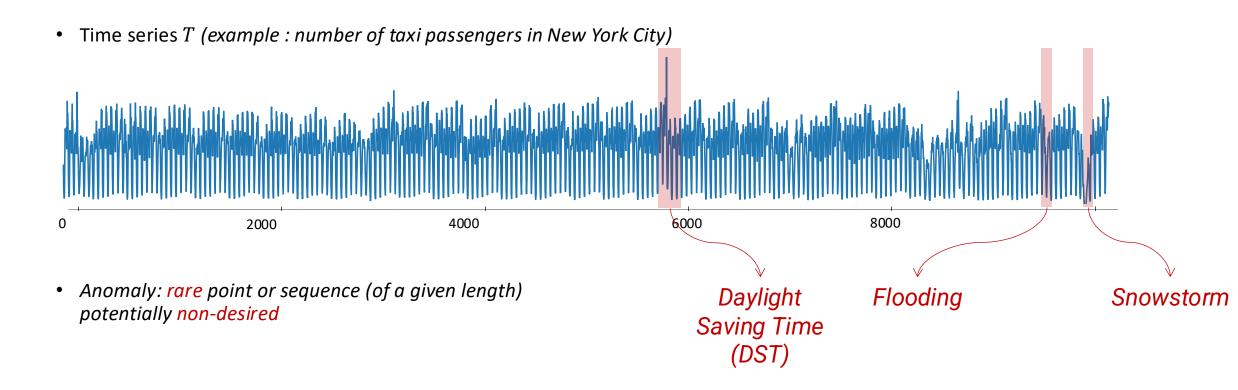
6000

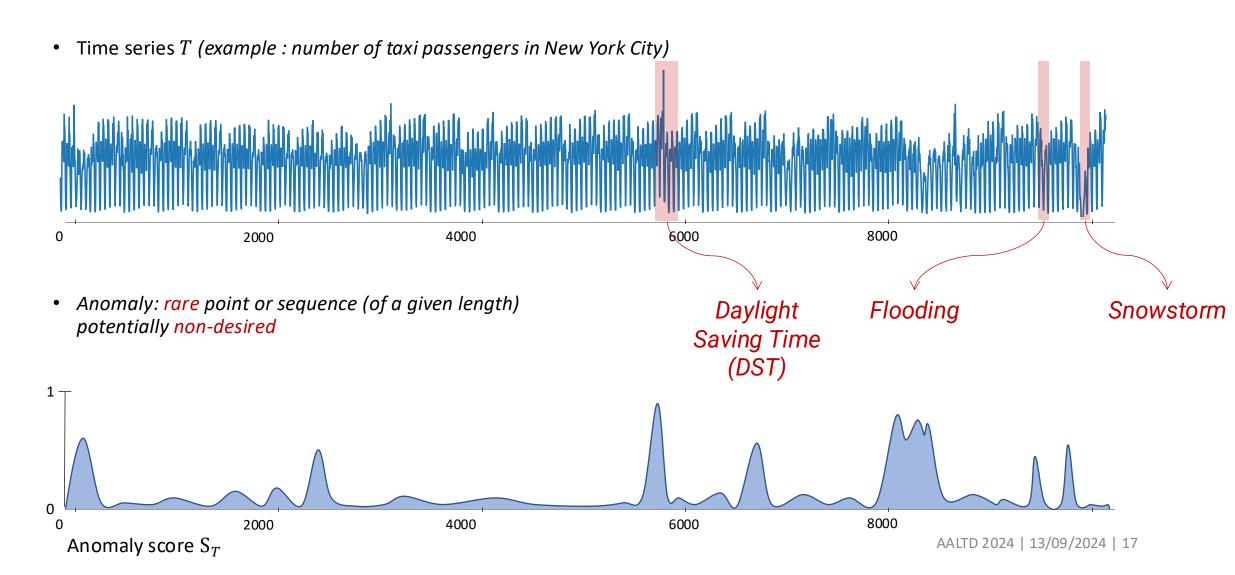
8000

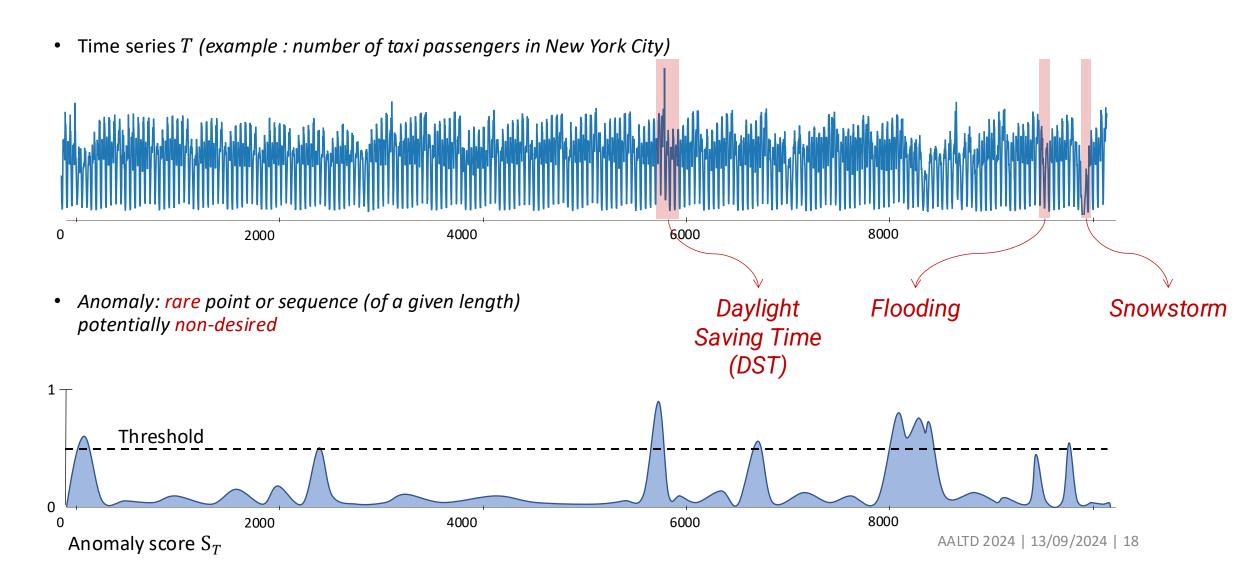
4000

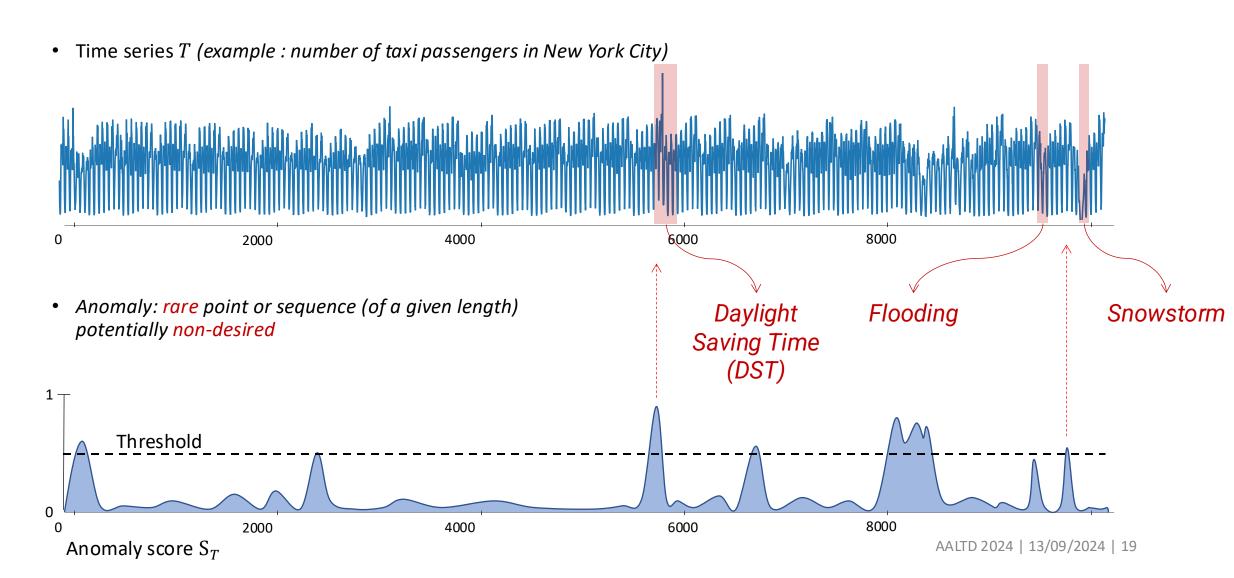
Anomaly: rare point or sequence (of a given length) potentially non-desired

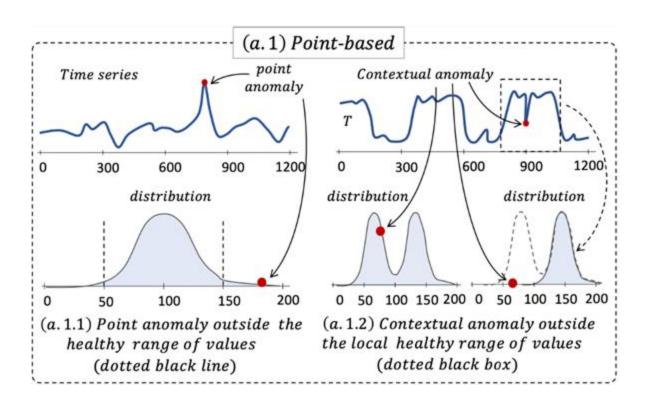
2000

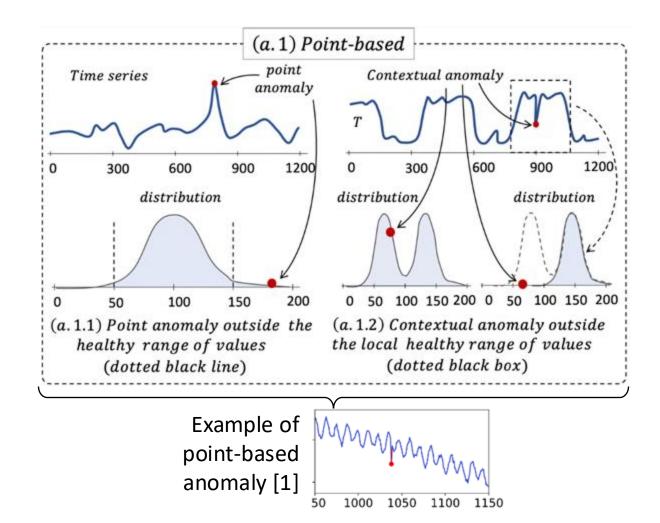


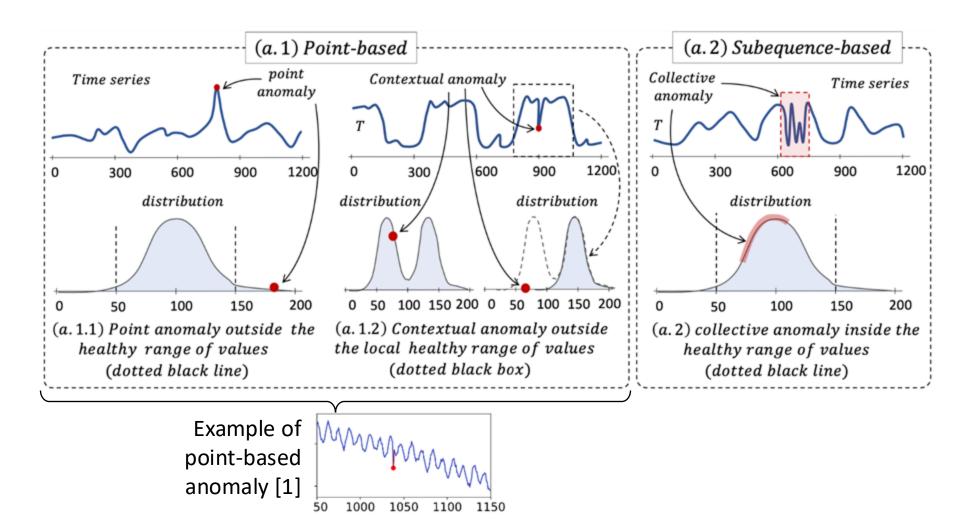


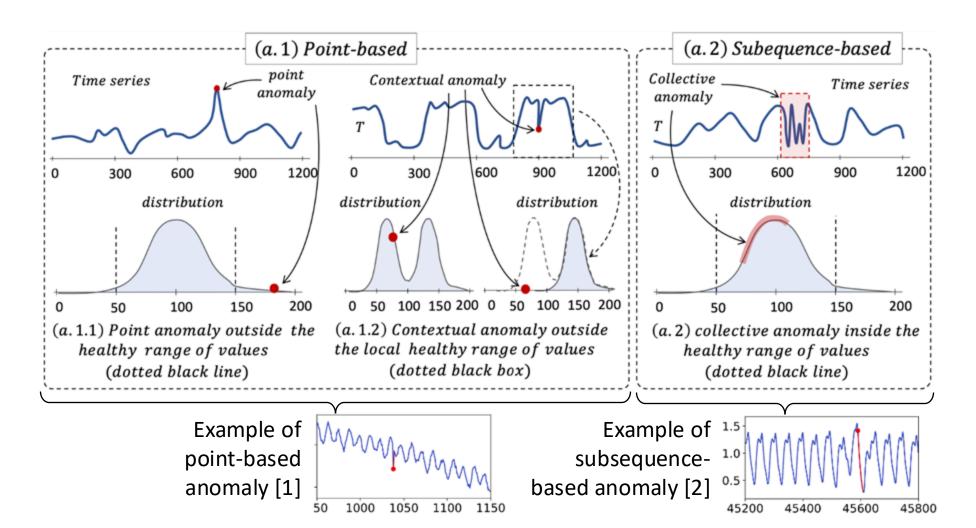


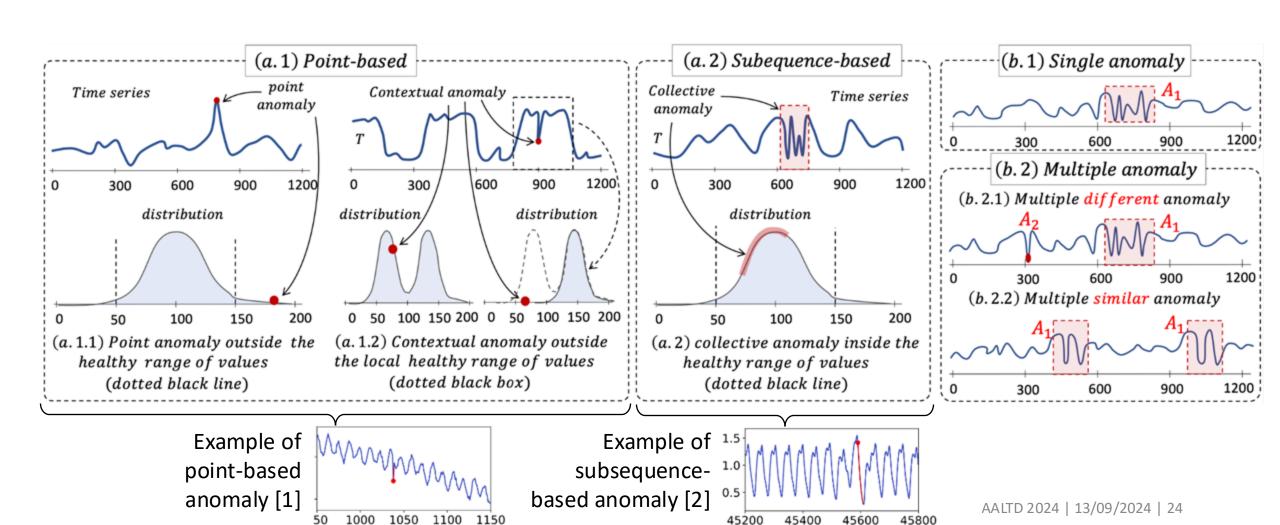












point

anomaly

1200

200

1000 1050 1100 1150

900

150

Example of

point-based

anomaly [1]

Time series

300

50

600

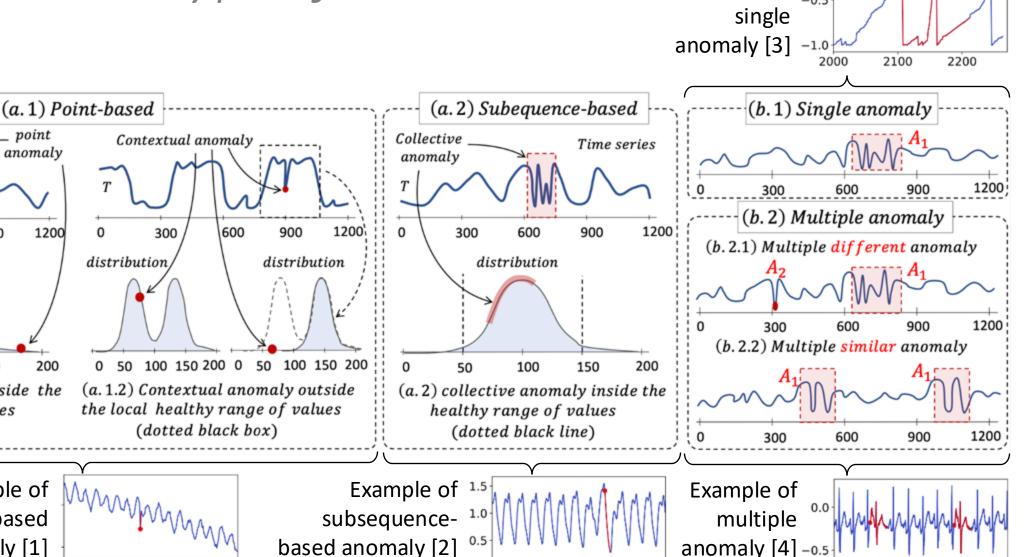
distribution

100

(a. 1.1) Point anomaly outside the

healthy range of values

(dotted black line)



45200

45400

45800

2500

2750

3000

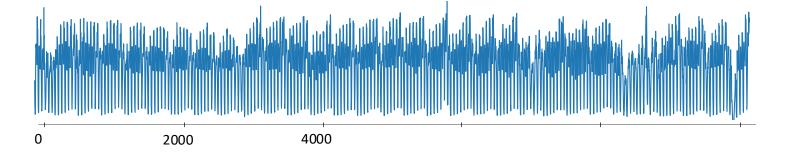
45600

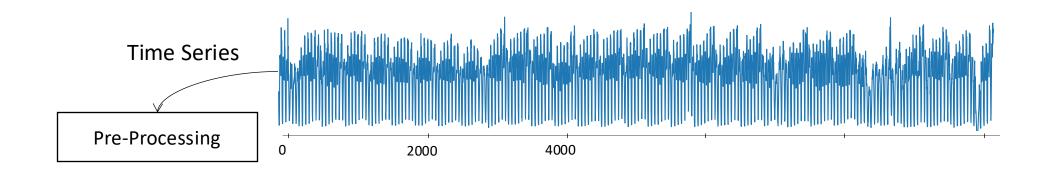
Example of

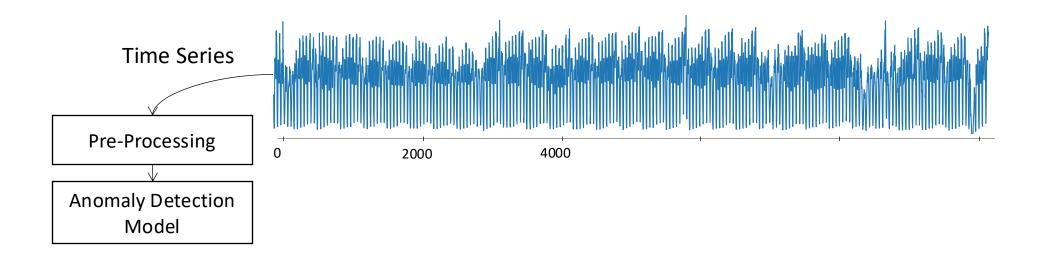
II. Time Series Anomaly Detection

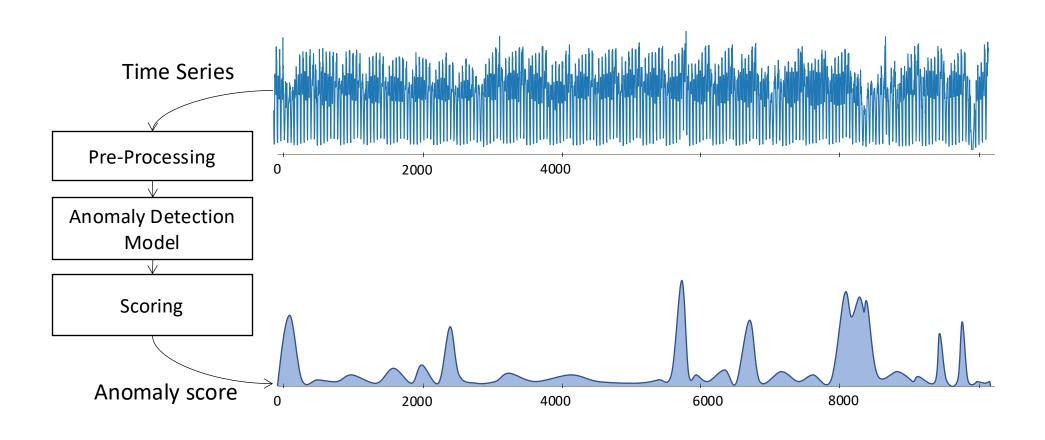
How does it work?

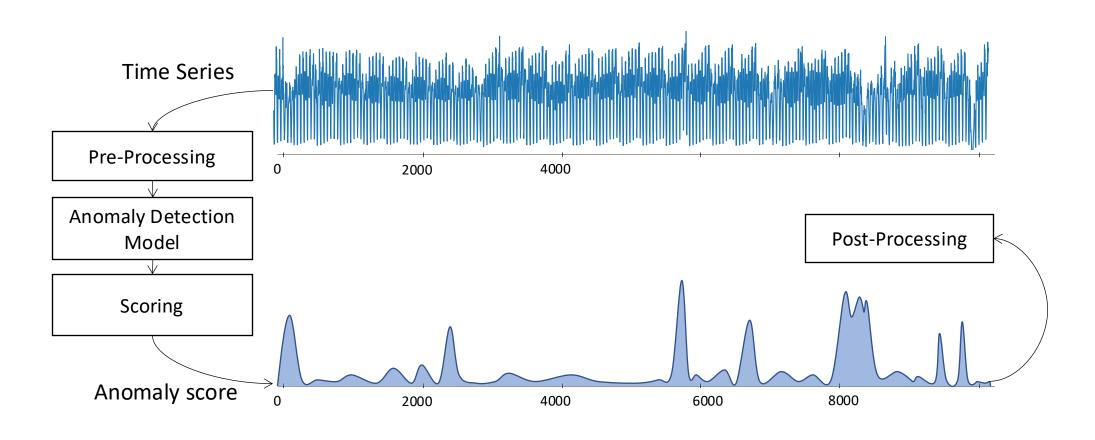


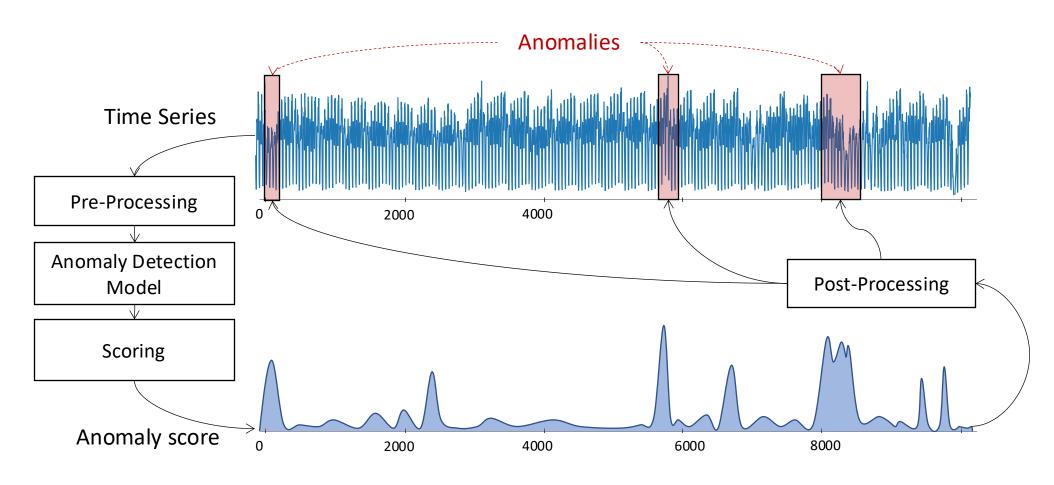


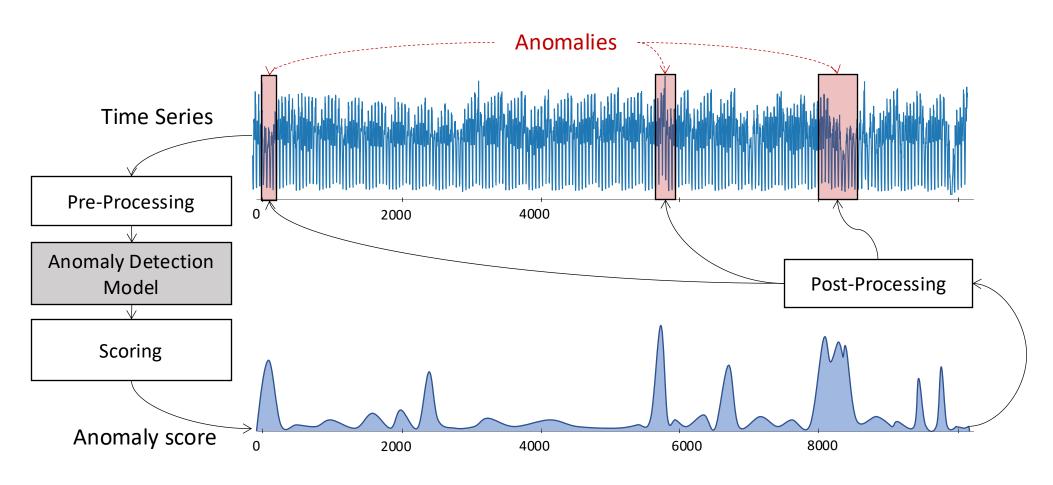




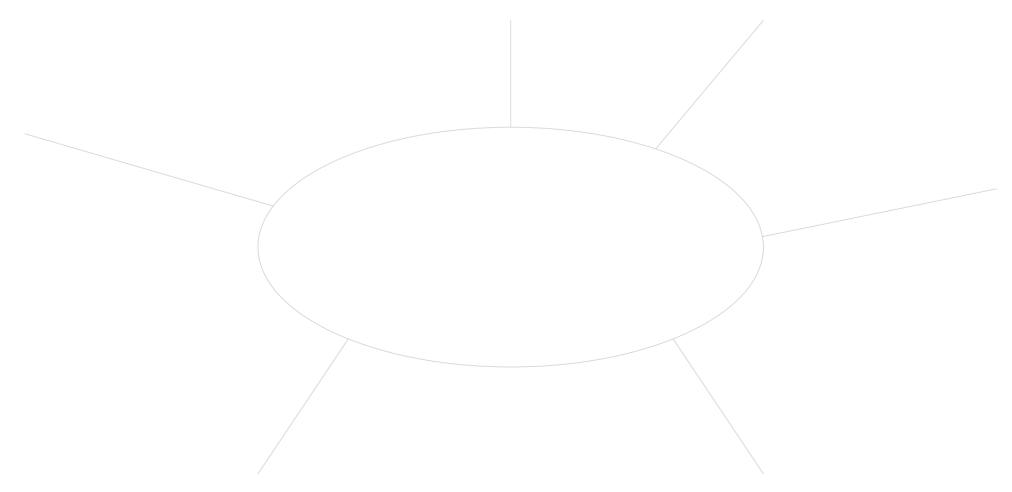




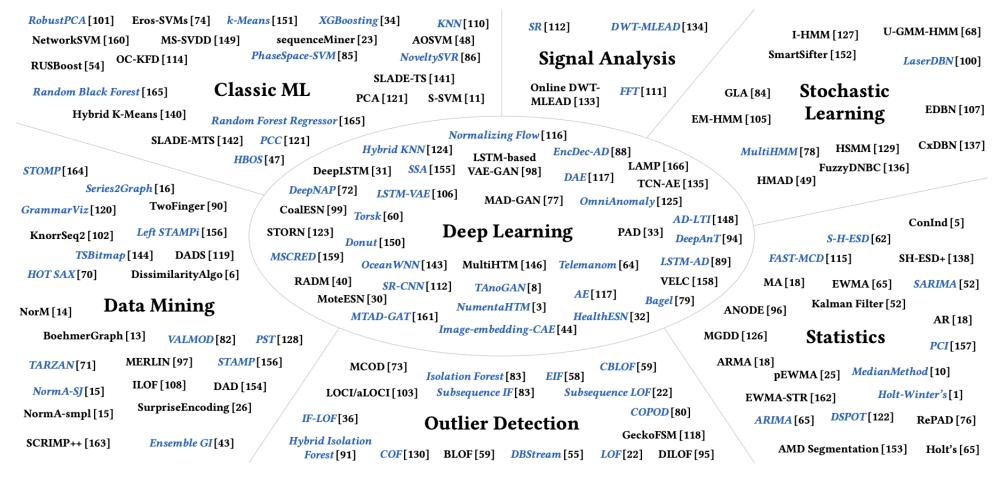




By domains [5] ...



By domains [5] ...



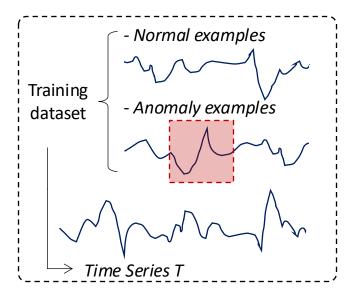
By inputs...

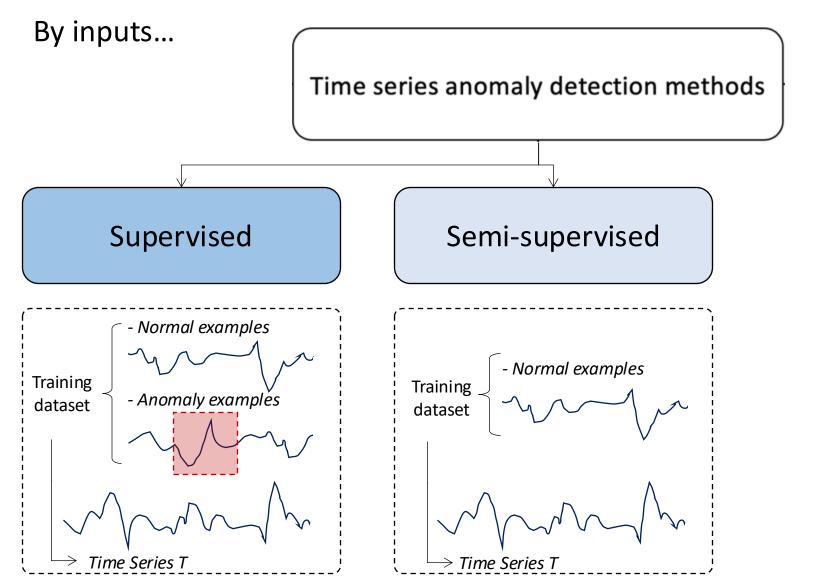
Time series anomaly detection methods

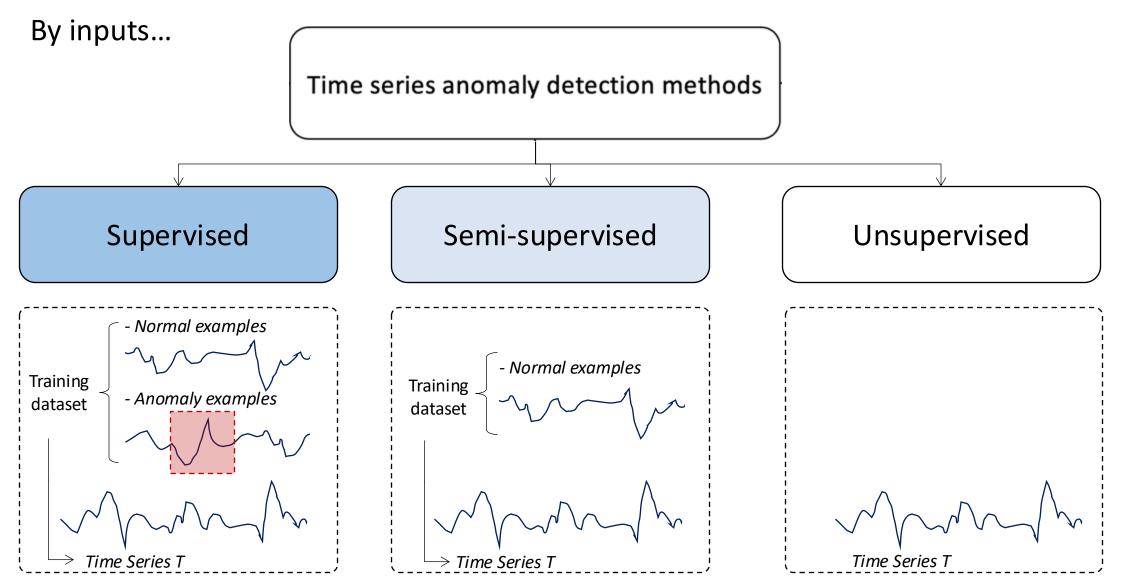
By inputs...

Time series anomaly detection methods

Supervised





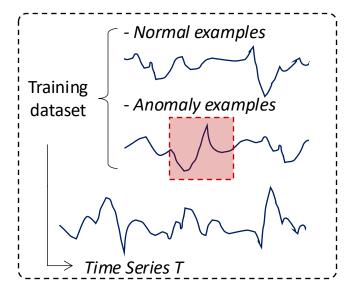


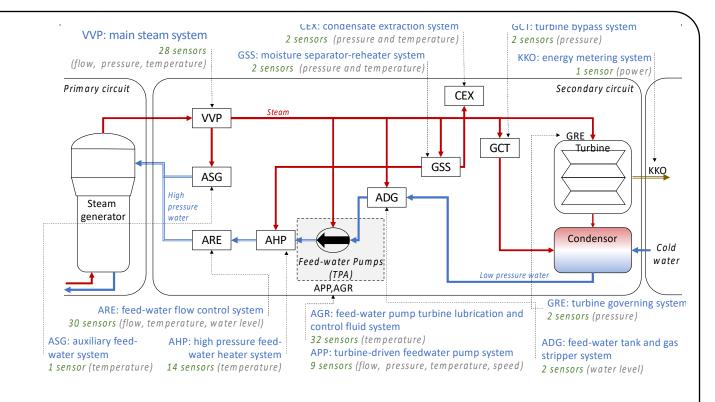
Anomaly Dete

By inputs...

Time

Supervised

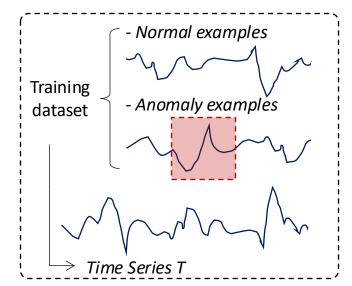




Anomaly Dete

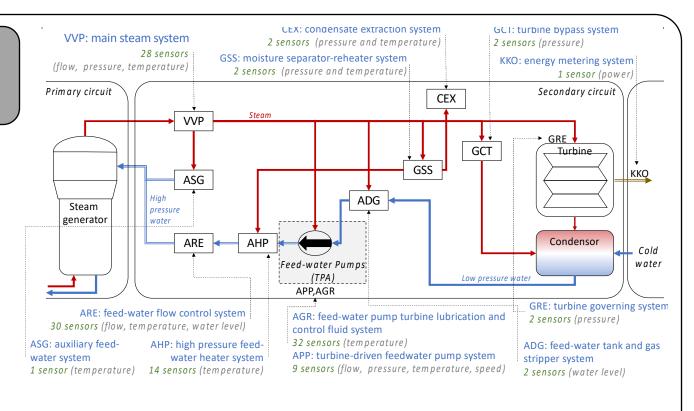
By inputs...

Supervised



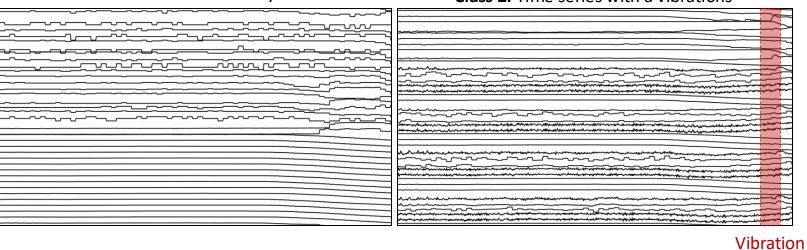
Supervised anomaly detection (e.g., classification)

Time



Class 1: Time series without any vibrations

Class 2: Time series with a vibrations



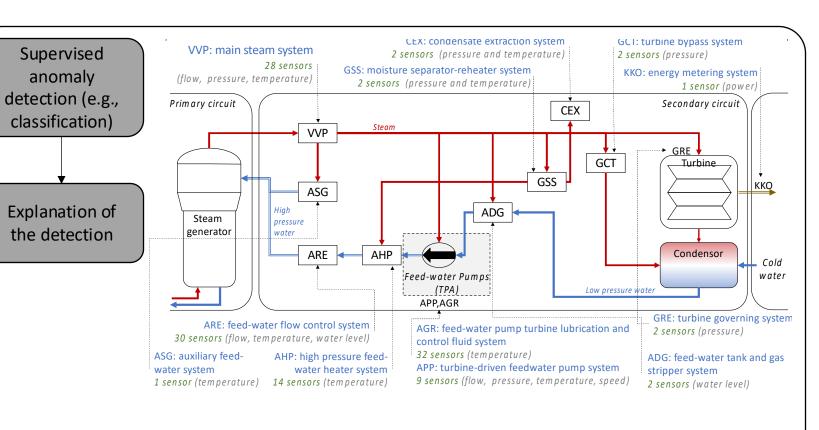
Anomaly Dete

By inputs...

Time

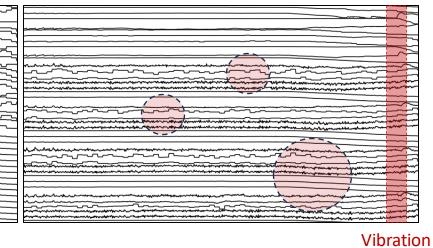
Supervised

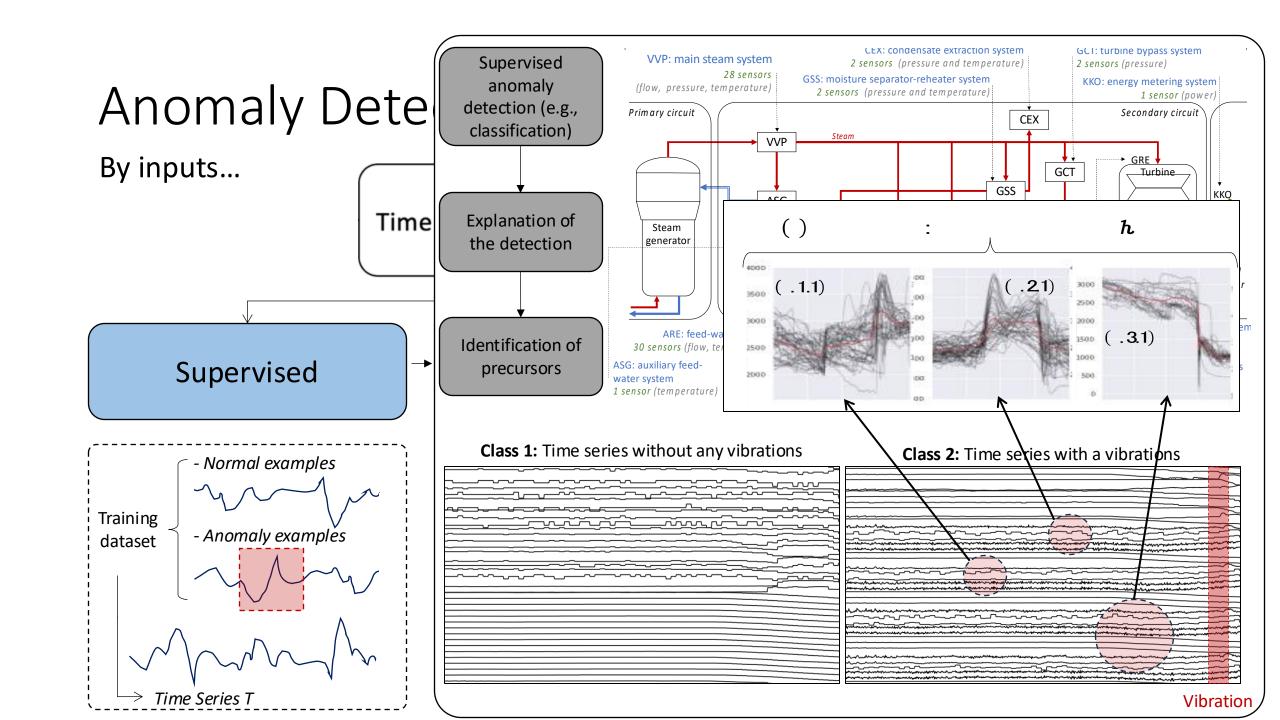
- Normal examples **Training** - Anomaly examples dataset Time Series T



Class 1: Time series without any vibrations

Class 2: Time series with a vibrations





Anomaly Dete Primary circuit By inputs... → GRE More info: Time On the method On the use case Supervised Class 1: Ti ations - Normal examples DCE journal 2023 SIGMOD 2022 **Training** - Anomaly examples DATA-CENTRIC ENGINEERING ACM SIGMOD dataset Time Series T

Vibration

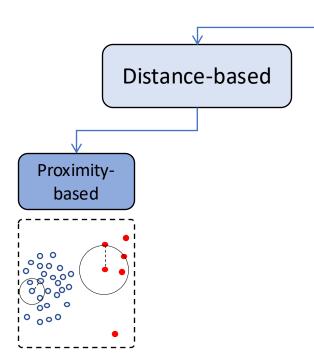
By methods...

By methods...

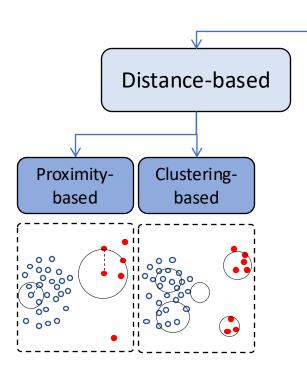
Time series anomaly detection methods

Distance-based

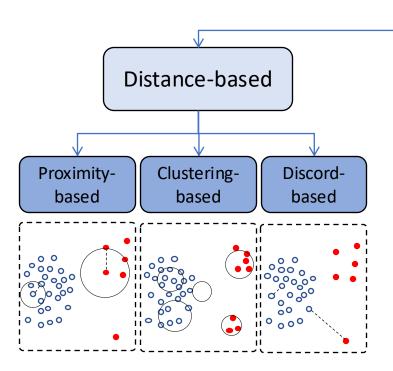
By methods...



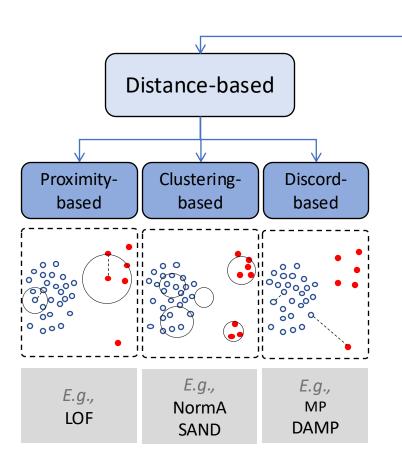
By methods...

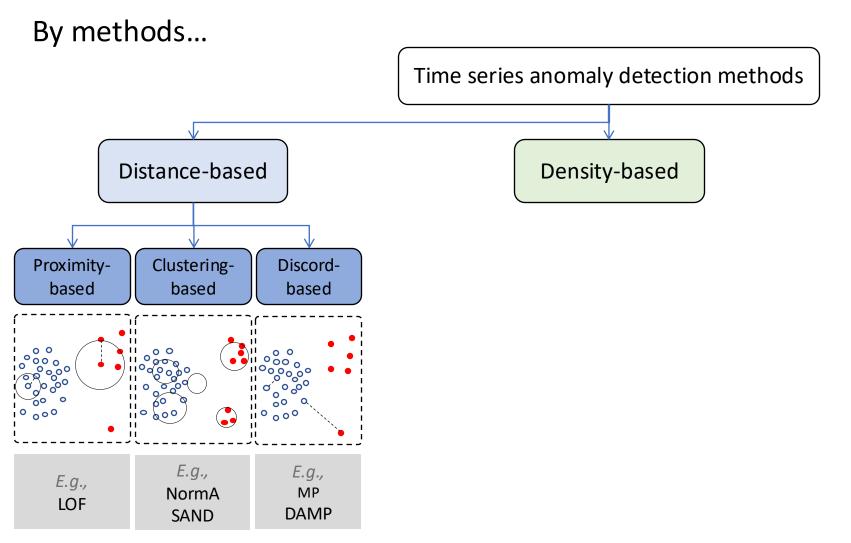


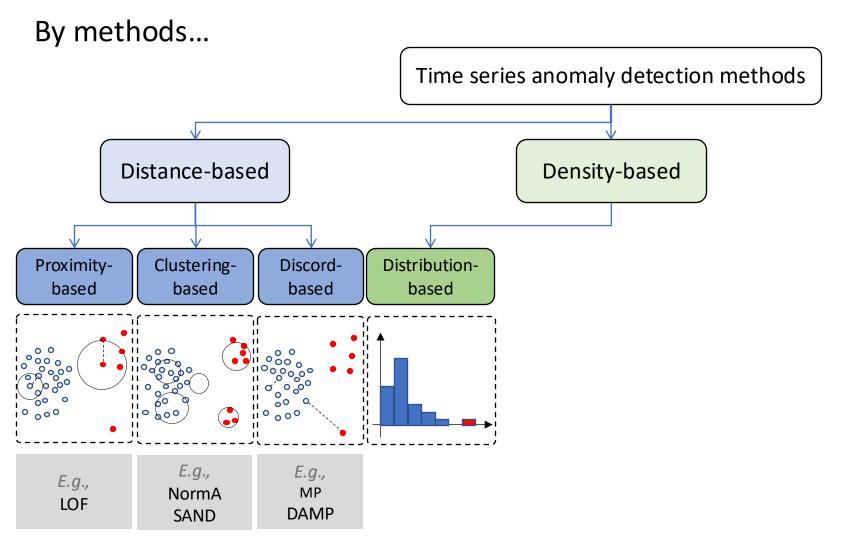
By methods...

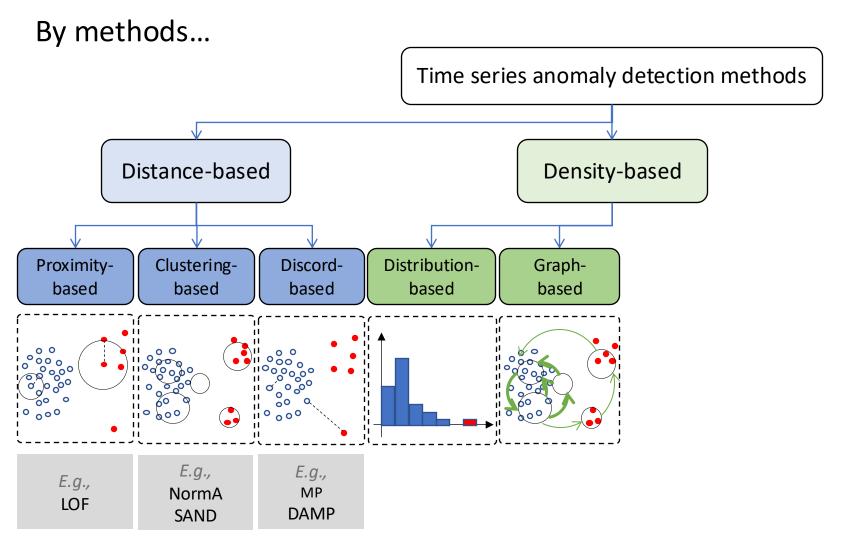


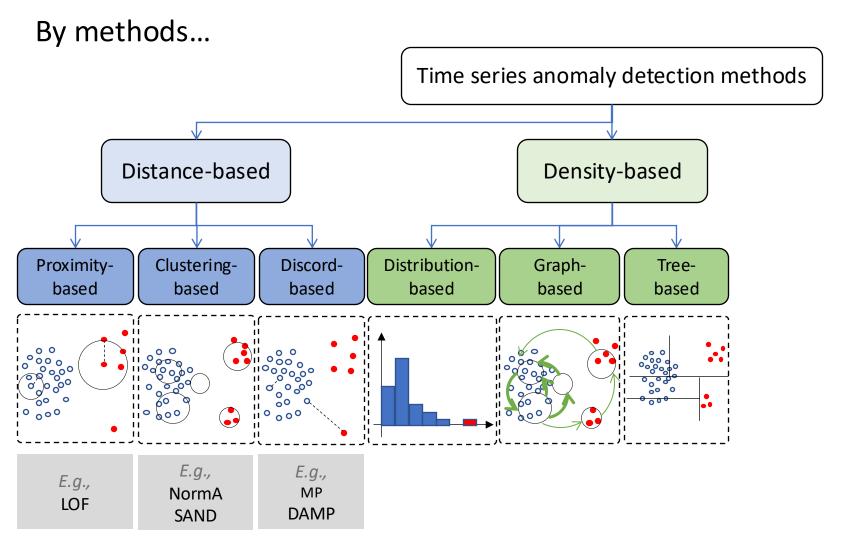
By methods...

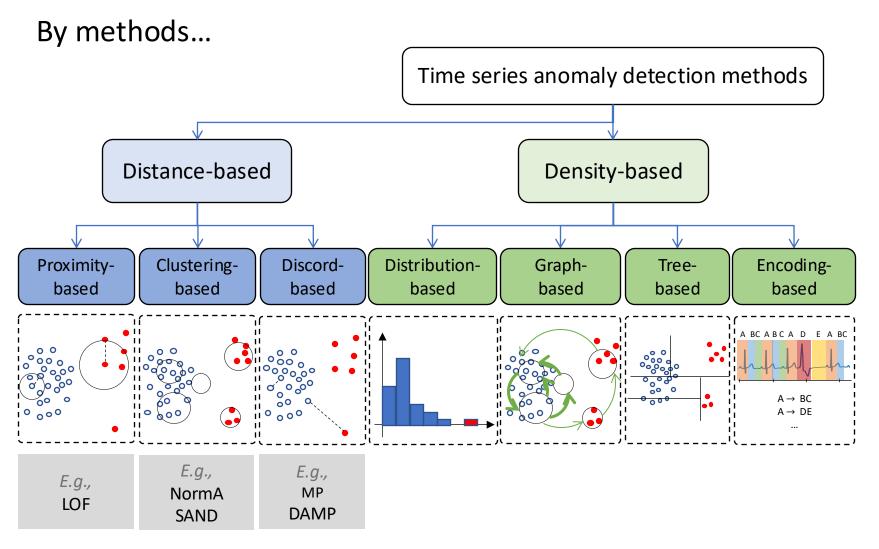


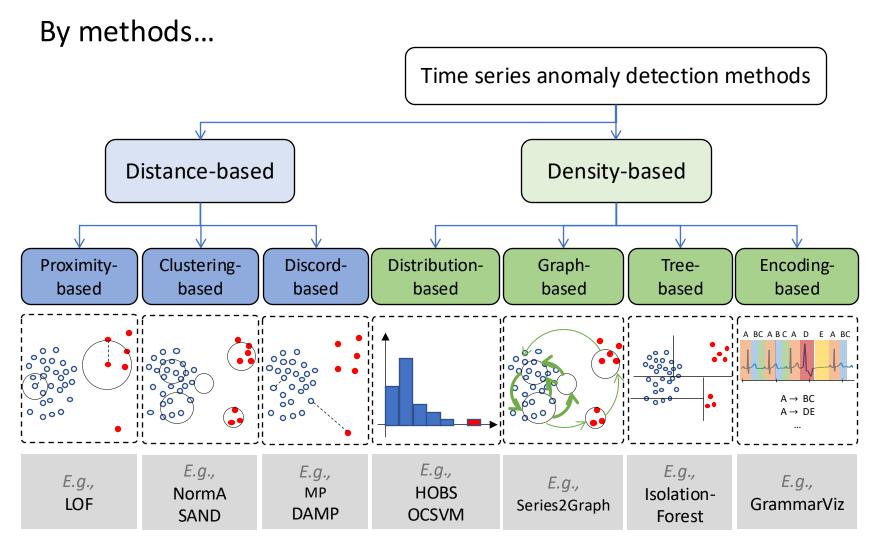


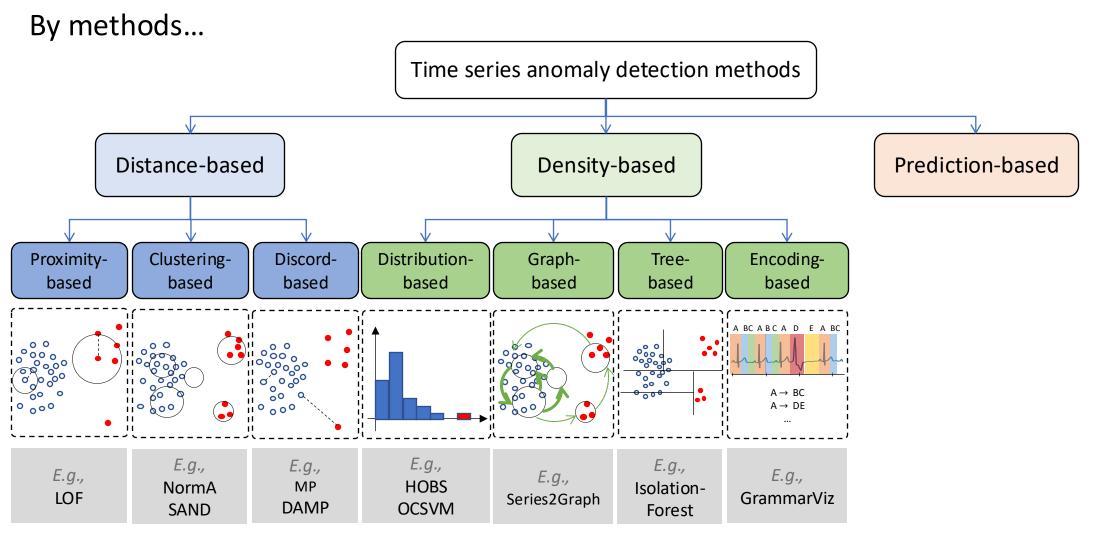


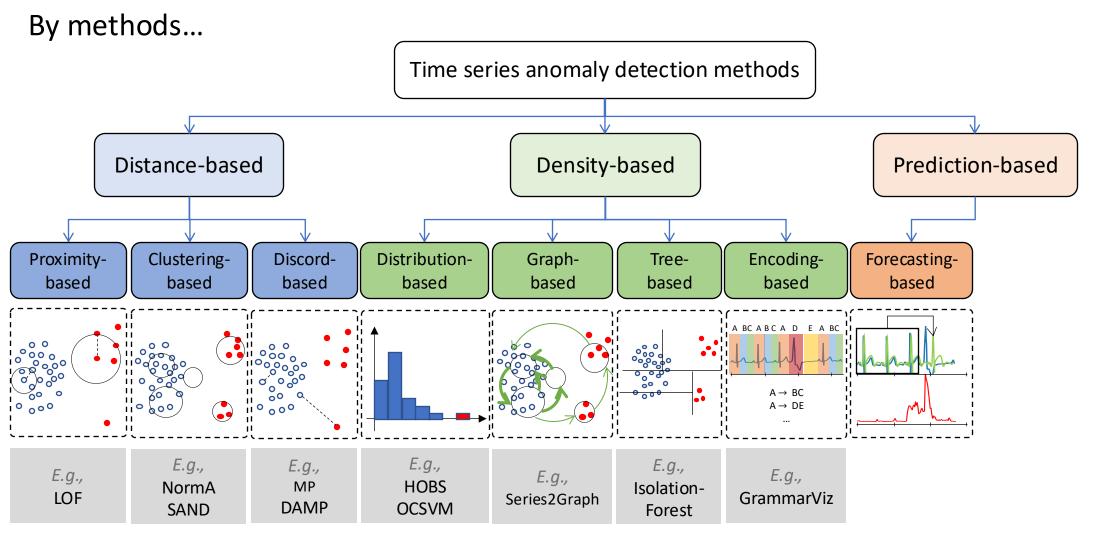


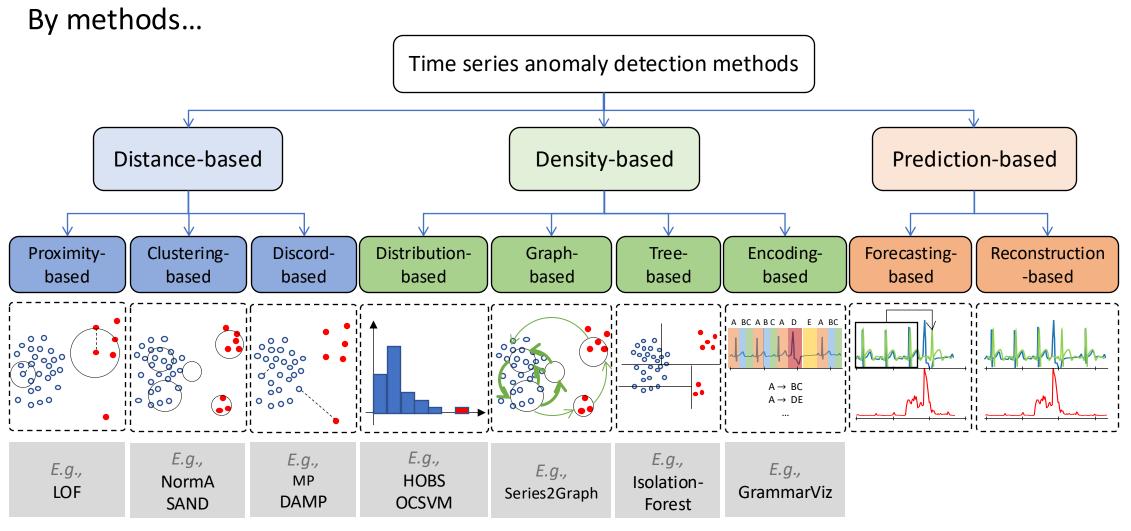


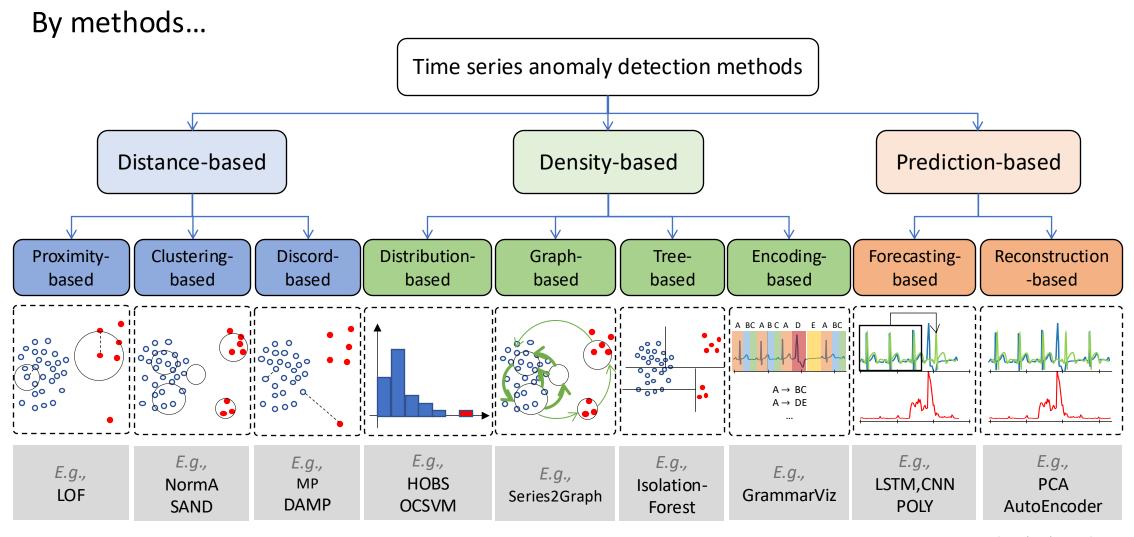




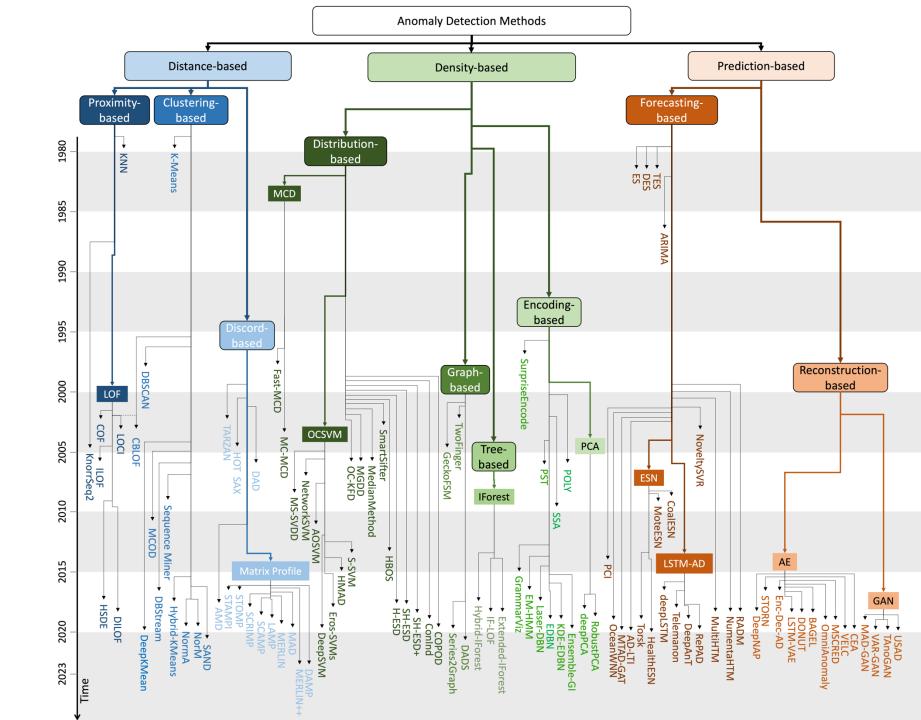


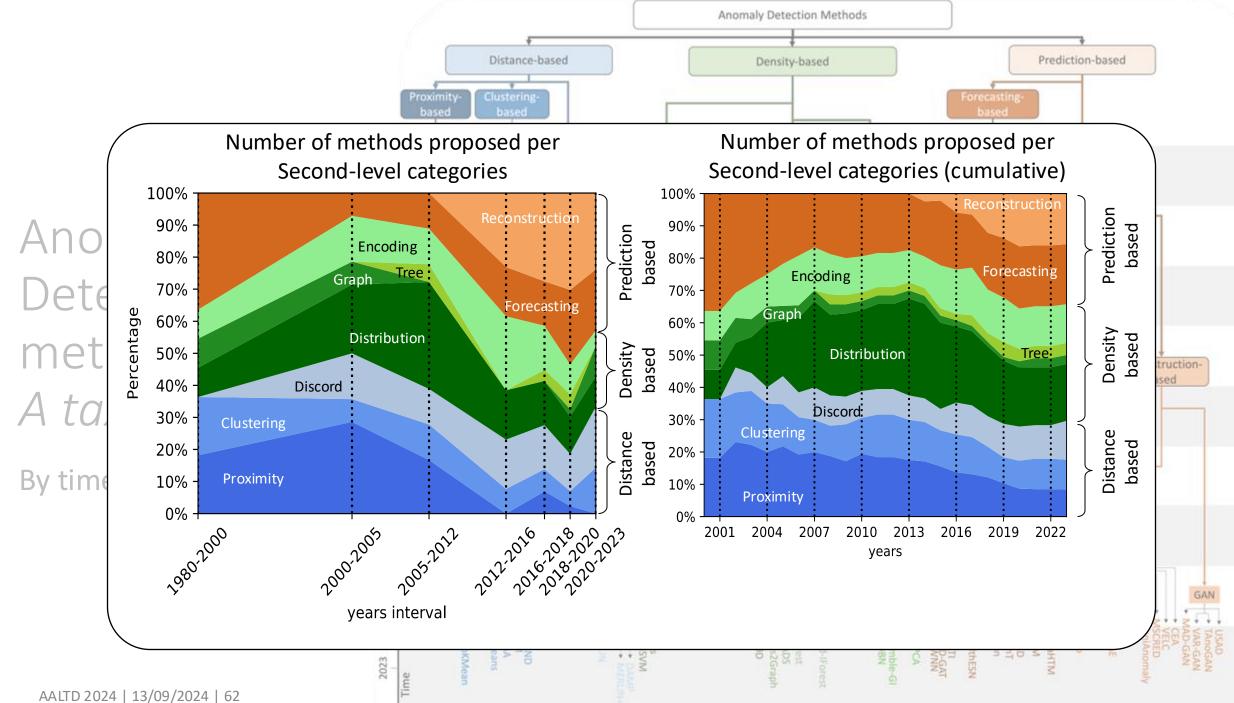


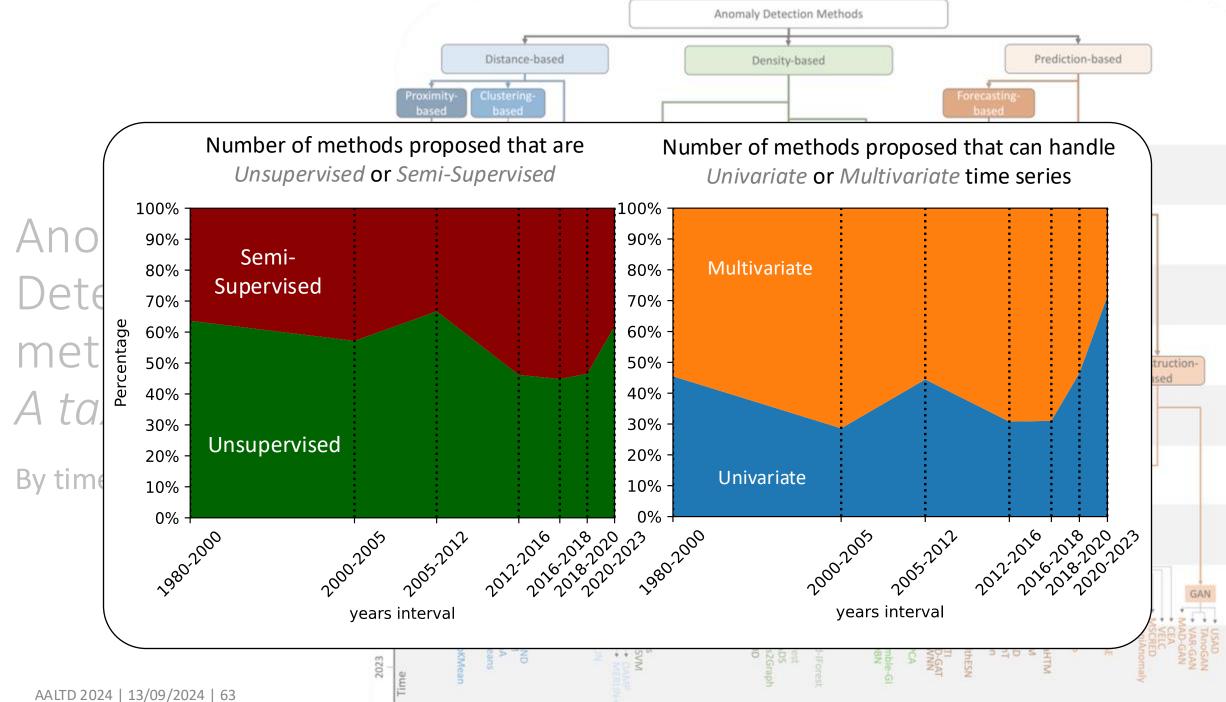


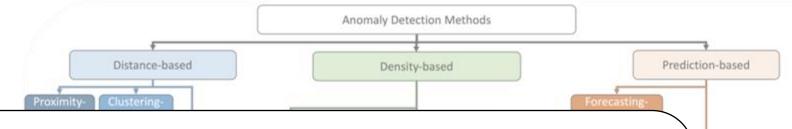


By time...









Time Series Anomaly Detection

Paul Boniol, Qinghua Liu, John Paparrizos, and Themis Palpanas.

Ano Dete met A ta.



Video (EDBT 2023 Tutorial)



https://www.youtube.com/watch?v=96869qimXAA&t=1s



Slides (VLDB 2024 Tutorial)



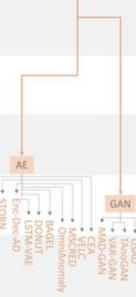
https://drive.google.com/file/d/1Vyz6 H0E16IpbVZXgtiZVnU9Ie8zAJaog/view



SIGMOD Blogpost

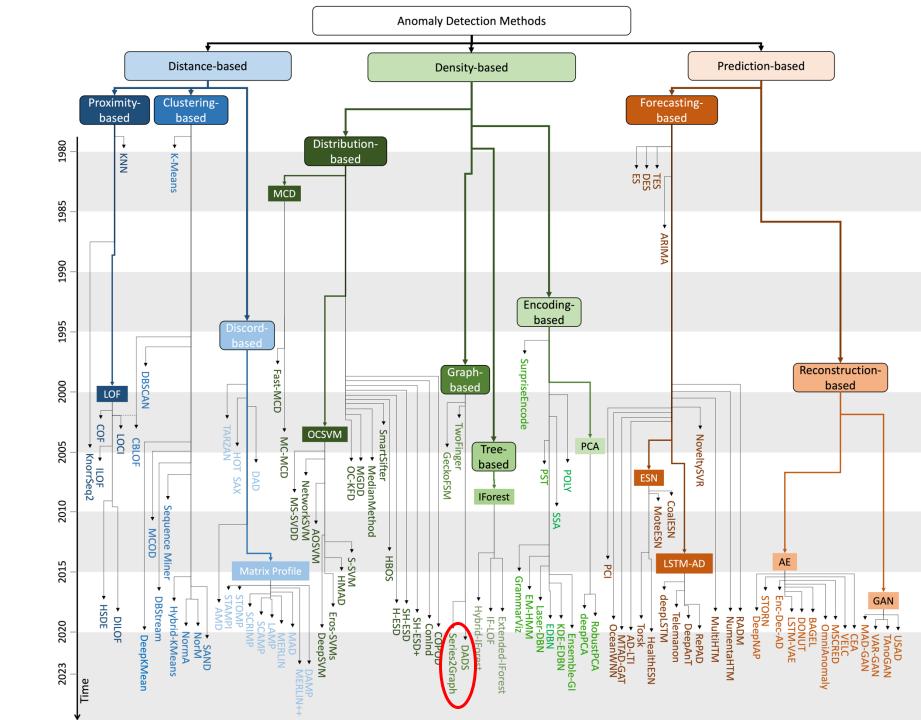


https://wp.sigmod.org/? p=3739



Reconstruction-

By time...

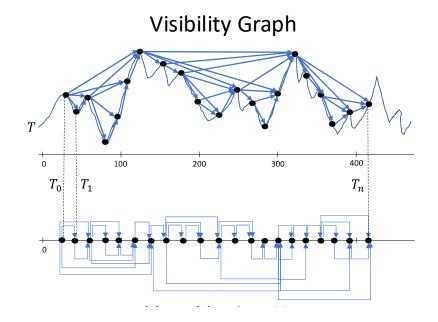


III. Series2Graph

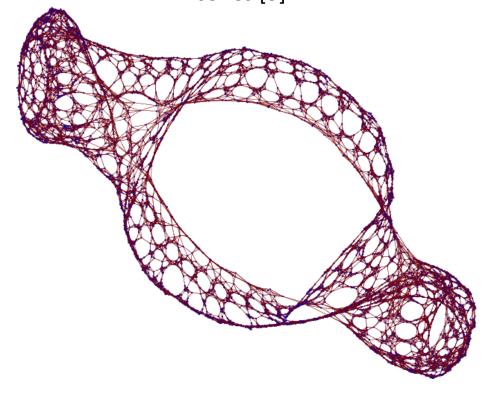
A graph-based approach

Converting the time series to a graph:

- Existing solutions create a node per point (e.g., Visibility Graph [6,7])
- Do not scale for large time series



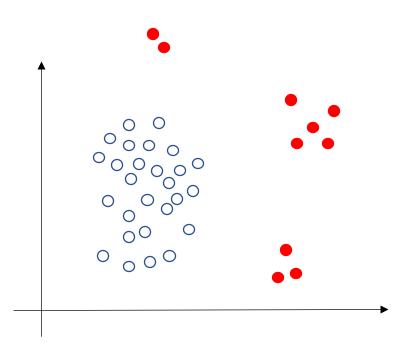
Complex network for time series [8]



M. Small et al. Transforming Time seires into Complex Networks, Complex Sciences (2009)

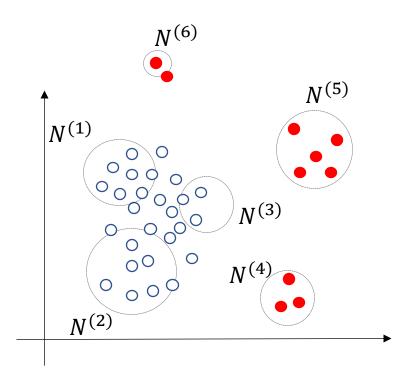
Graph G_{ℓ_G} [9]:

Given a data series T, and an input length ℓ_G , we build a graph $G_{\ell_G}(\mathcal{N}, \mathcal{E})$ for which:



Graph G_{ℓ_G} [9]:

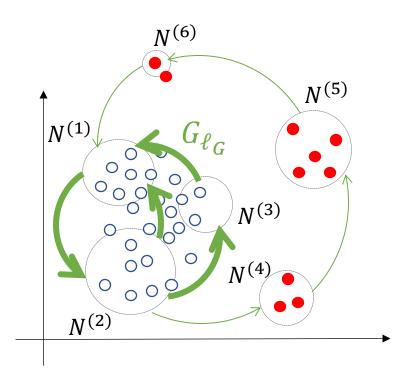
Given a data series T, and an input length ℓ_G , we build a graph $G_{\ell_G}(\mathcal{N}, \mathcal{E})$ for which:



Each node is an ensemble of similar subsequences.

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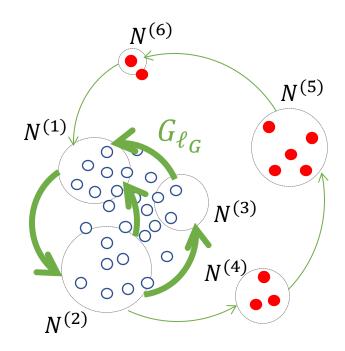
Each node is an ensemble of similar subsequences.

Each edge is associated to a weight w that corresponds to the number of times a subsequence move from one node to another.

A subsequence $T_{i,\ell}$ (with $\ell > \ell_G$) is a path in G_{ℓ_C} .

Graph G_{ℓ_G} [9]:

Given a data series T, and an input length ℓ_G , we build a graph $G_{\ell_G}(\mathcal{N}, \mathcal{E})$ for which:

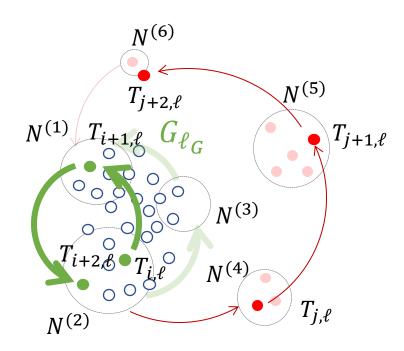


For a given subsequence $T_{i,\ell}$ and its corresponding path $P_{th} = \langle N^{(i)}, N^{(i+1)}, ..., N^{(i+\ell)} \rangle$, we define the normality score as follows: $\sum_{i+\ell-1} w(N^{(j)}, N^{(j+1)}) \deg(N^{(j)} - 1)$

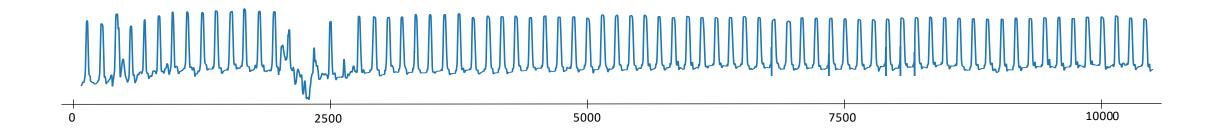
$$Norm(P_{th}) = \sum_{j=i}^{N} \frac{w(N^{j}, N^{j}) \operatorname{deg}(N^{j-1})}{\ell}$$

Graph G_{ℓ_G} [9]:

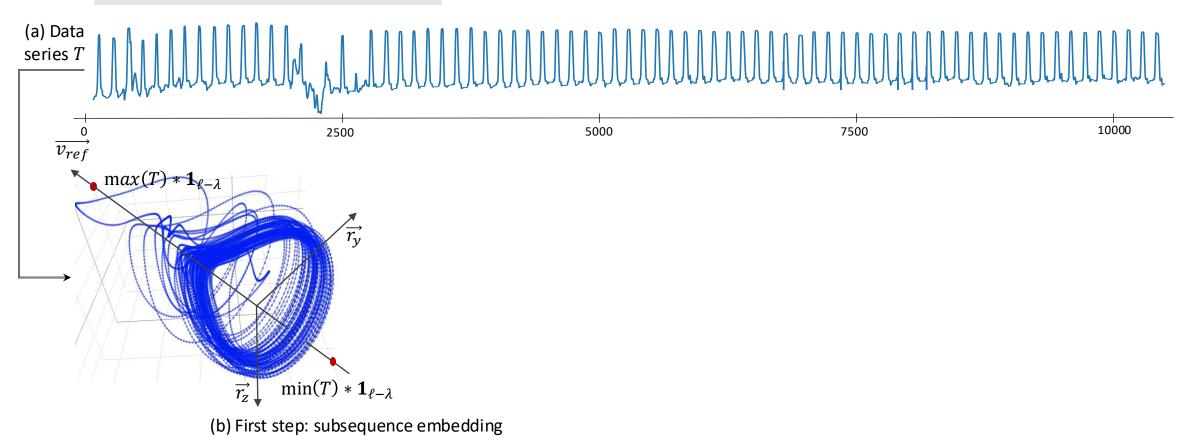
Given a data series T, and an input length ℓ_G , we build a graph $G_{\ell_G}(\mathcal{N}, \mathcal{E})$ for which:



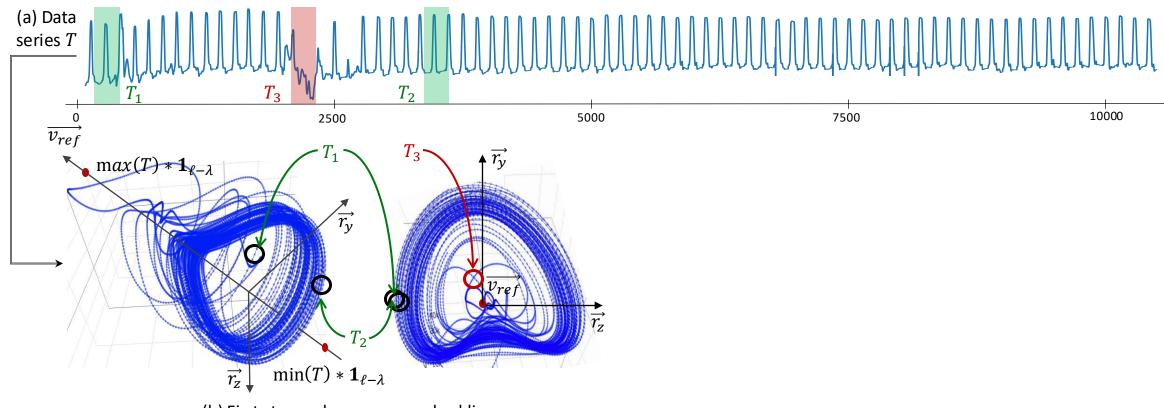
$$Norm\left(P_{th}(T_{j,\ell+2})\right) \ll Norm\left(P_{th}(T_{i,\ell+2})\right)$$



3 components of the *Principal Component Analysis* applied on all subsequences of *T*

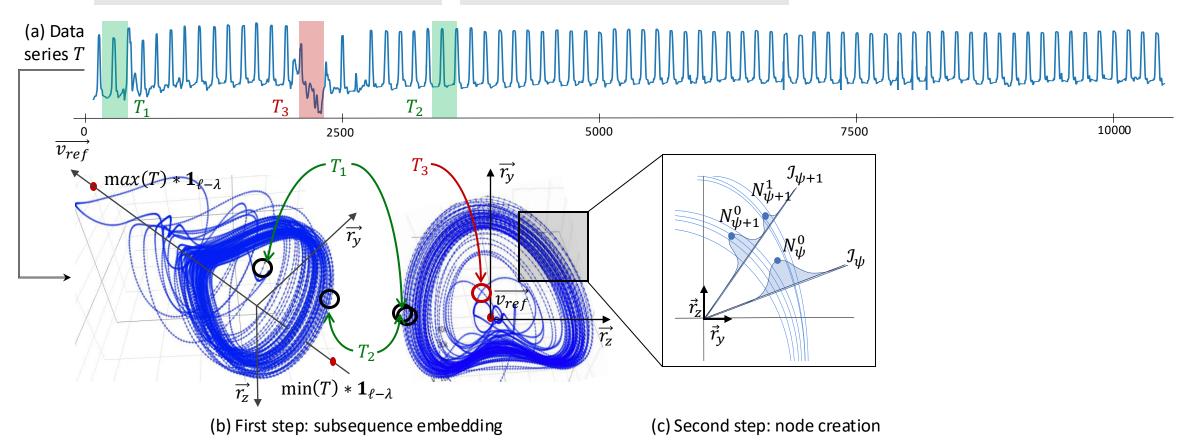


3 components of the *Principal Component Analysis* applied on all subsequences of *T*

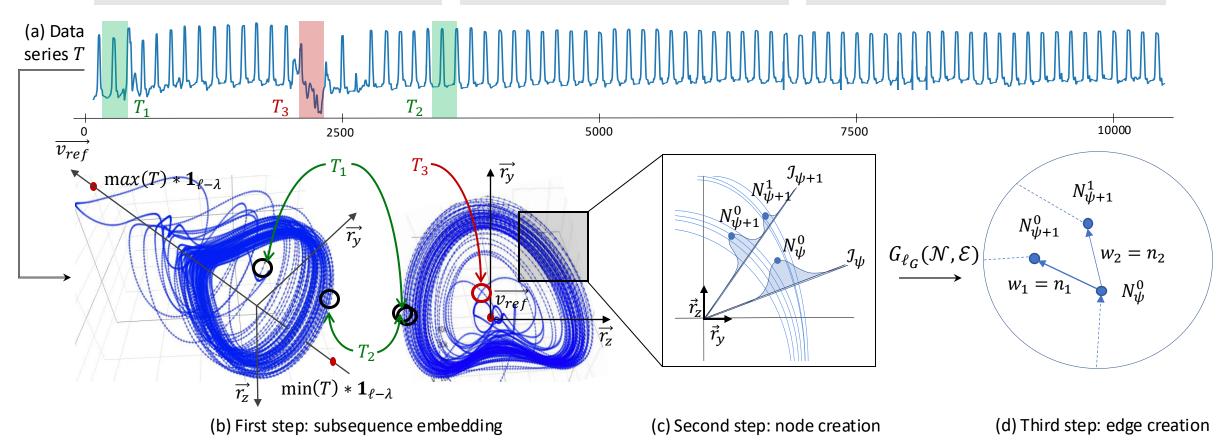


(b) First step: subsequence embedding

- 3 components of the *Principal Component Analysis* applied on all subsequences of *T*
- Gaussian density estimation on each radius (among a fixed number of radius)

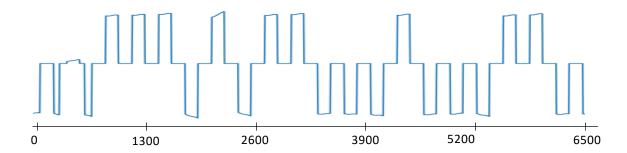


- 3 components of the *Principal Component Analysis* applied on all subsequences of *T*
- Gaussian density estimation on each radius (among a fixed number of radius)
- Assign each subsequence to a node and set an edge for each transition between nodes

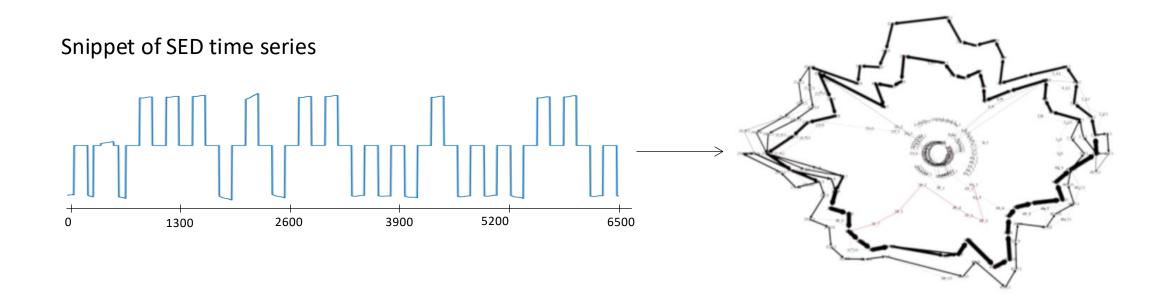


Series2Graph: An Example

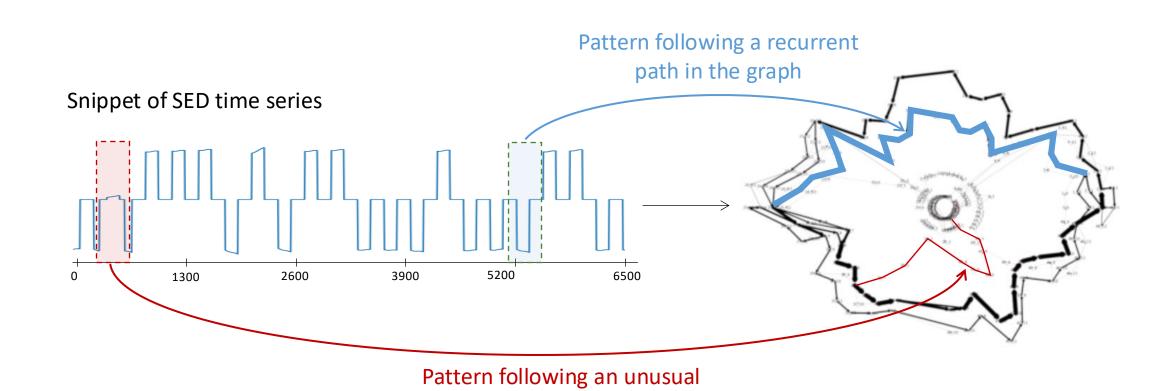
Snippet of SED time series



Series2Graph: An Example



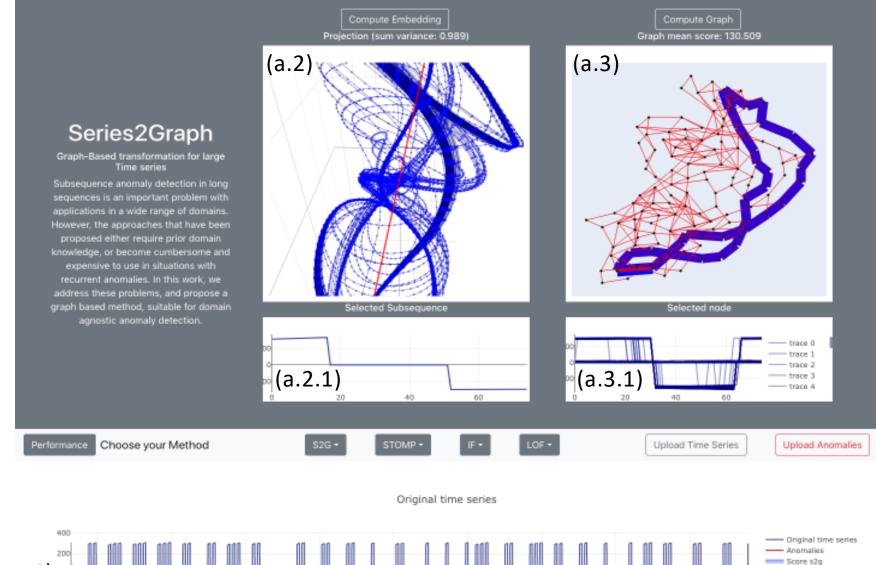
Series2Graph: An Example

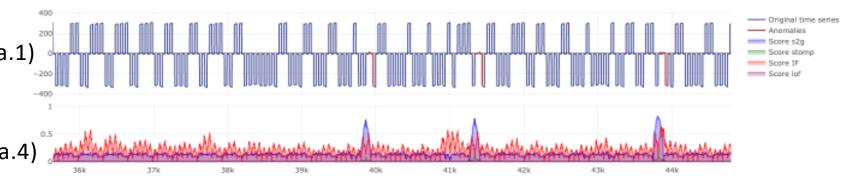


path in the graph

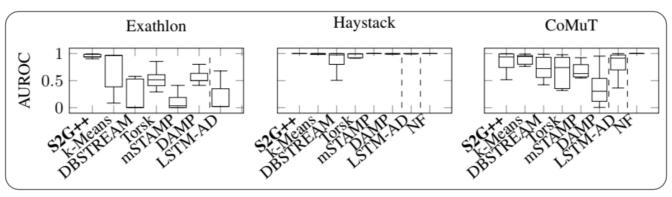
Series2Graph: *An interactive tool*

GraphAn: S2G User interface [10]





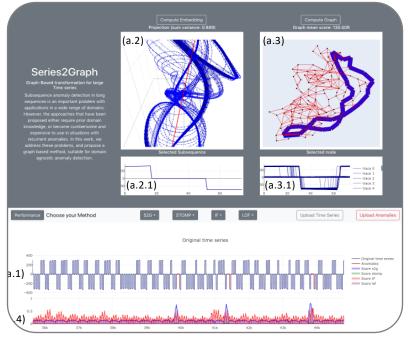
Series2Graph: To conclude



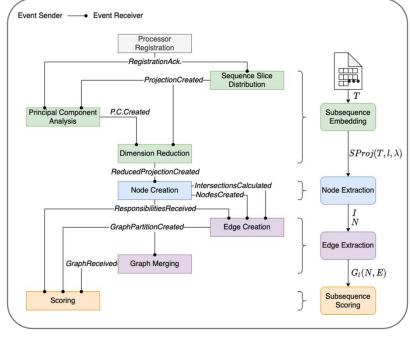
Series2Graph++: Multivariate extension of S2G [11]

In summary:

- We proposed a user interface to explore the resulting graph [10]
- Series2Graph extensions have been proposed [11,12]



GraphAn: S2G User interface [10]



DADS: Distributed version of S2G [12]

Several research directions

 Can the graph structure of Series2Graph help identify different time series types?

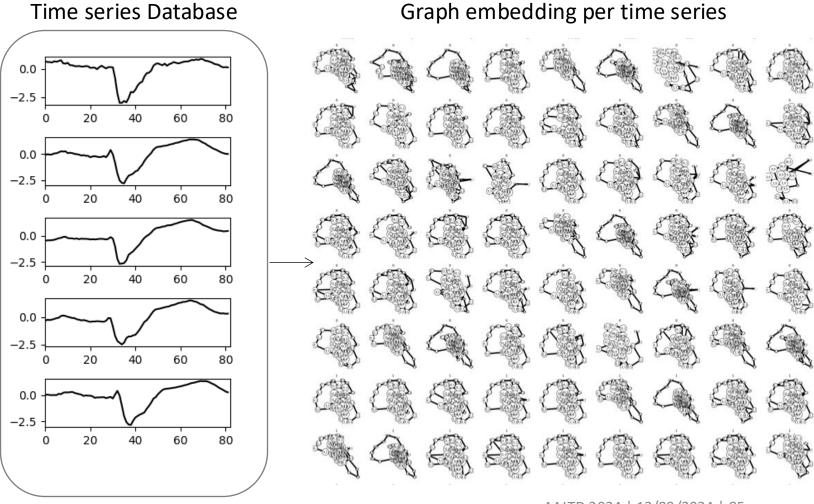
Several research directions

Can the graph structure of Series2Graph help identify different time series types?

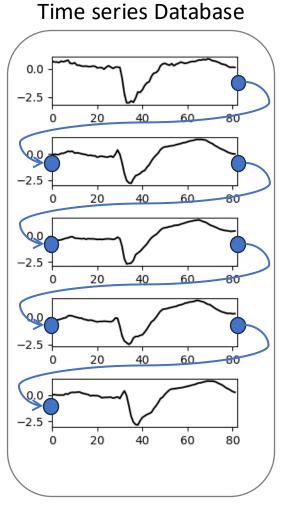
Time series Database 0.0 -2.560 -2.560 -2.560 -2.520 60 -2.520

Several research directions

 Can the graph structure of Series2Graph help identify different time series types?

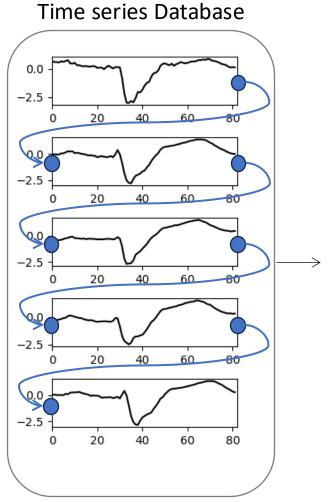


- Can the graph structure of Series2Graph help identify different time series types?
- Is a unique graph meaningful for a set of time series?

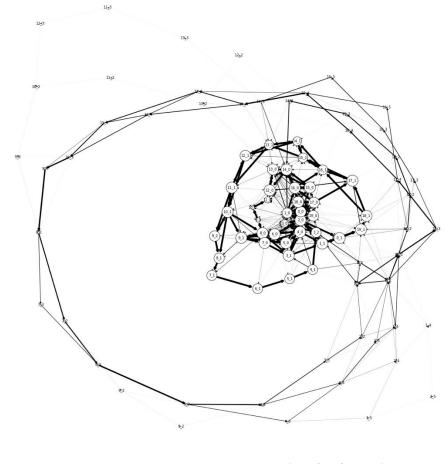


Several research directions

- Can the graph structure of Series2Graph help identify different time series types?
- Is a unique graph meaningful for a set of time series?

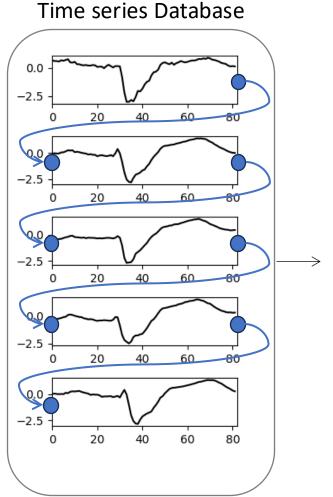


Graph embedding of the database

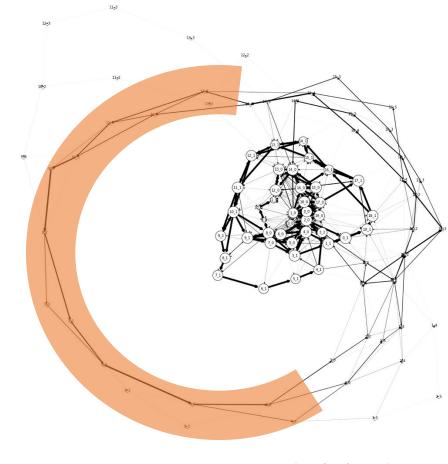


Several research directions

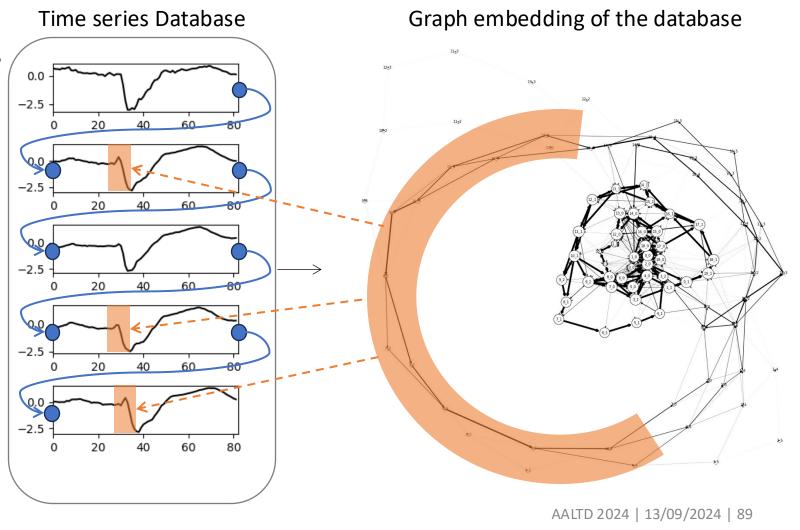
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Graph embedding of the database



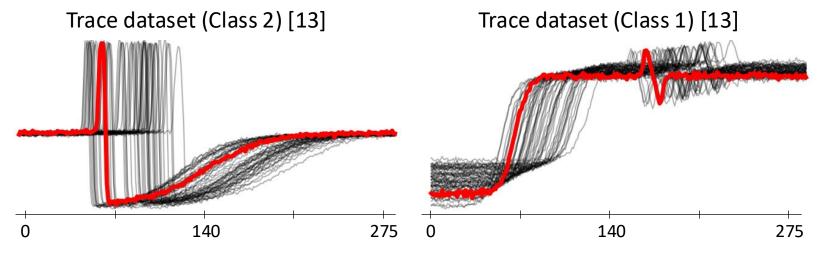
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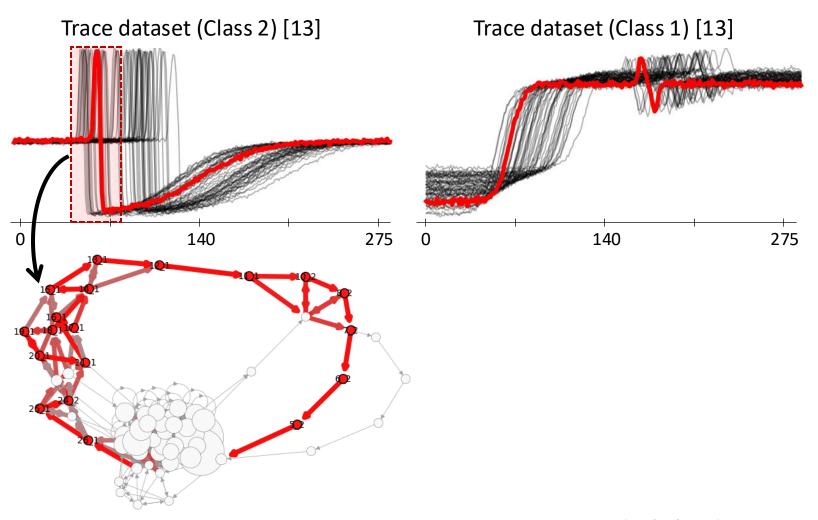
Several research directions

Can the graph structure of Series2Graph help identify different time series types?

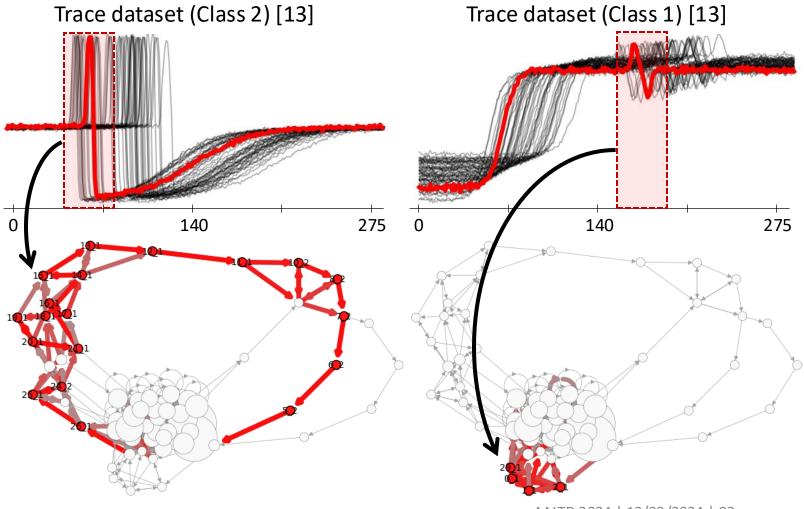
Is a unique graph meaningful for a set of time series?



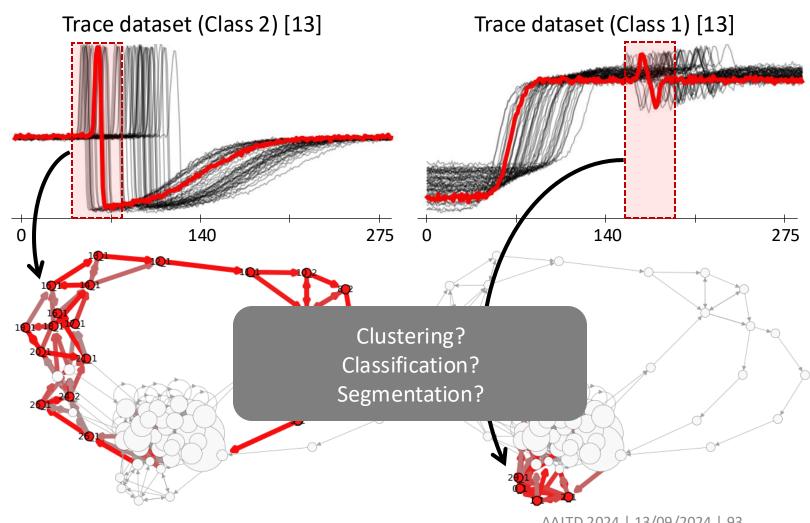
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- Can the graph structure of Series2Graph help identify different time series types?
- Is a unique graph meaningful for a set of time series?



- Can the graph structure of Series2Graph help identify different time series types?
- Is a unique graph meaningful for a set of time series?
- Can we use this graph to perform multiple analytics?



Series2Graph: Seve Graph-based Subsequence Anomaly Detection in Time Series Paul Boniol and Themis Palpanas. Ca Ser 275 GitHub Repositories Paper Is a (VLDB 2020) TSB-UAD **DADS** S2Gpp Ca pe **HPI-Information**https://www.vldb.org/pvldb TheDatumOrg/ **HPI-Information-**/vol13/p1821-boniol.pdf Systems/DADS Systems/S2Gpp TSB-UAD

IV. Automated Solutions

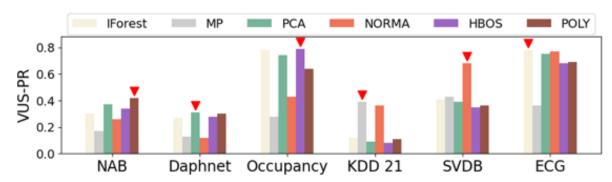
How to pick automatically the best method?

Automated Solution: Background

Motivation:

No one-size-fits-all model: How can we automatically identify the best anomaly detector given a time series?

Detection accuracy (VUS-PR) for 6 anomaly detectors across different datasets in TSB-UAD [14]

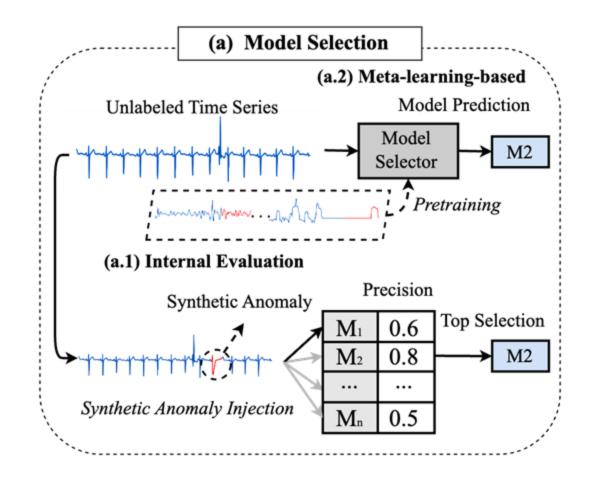


Automated Solution: Taxonomy

(a) Model Selection:

Selecting the best anomaly detector from a predefined candidate model set.

- (a.1) Internal Evaluation
- (a.2) Meta-learning-based



Automated Solution: *Taxonomy*

(a) Model Selection:

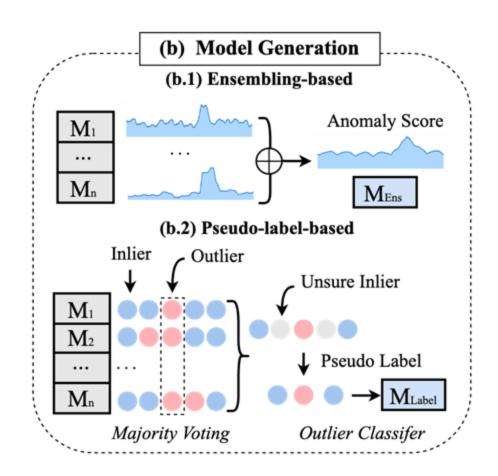
Selecting the best anomaly detector from a predefined candidate model set.

- (a.1) Internal Evaluation
- (a.2) Meta-learning-based

(b) Model Generation:

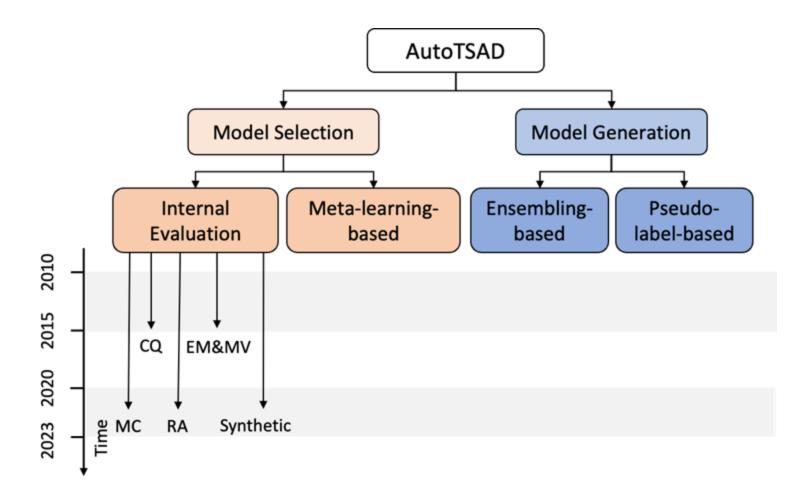
Creating an entirely new model for the given time series based on the candidate mode set

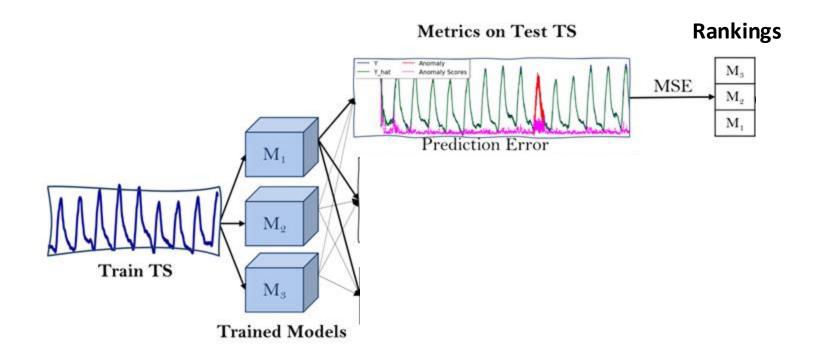
- (b.1) Ensembling-based
- (b.2) Pseudo-label-based

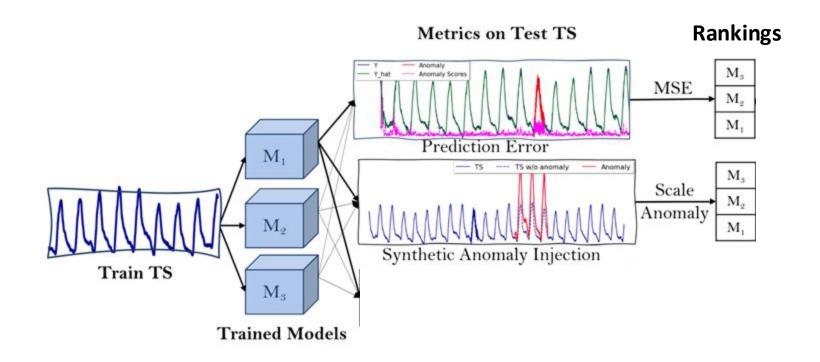


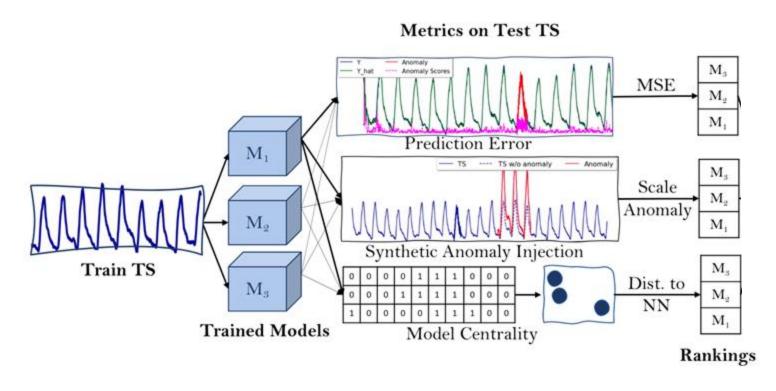
Definition: Evaluate the effectiveness of a model without any reliance on external information

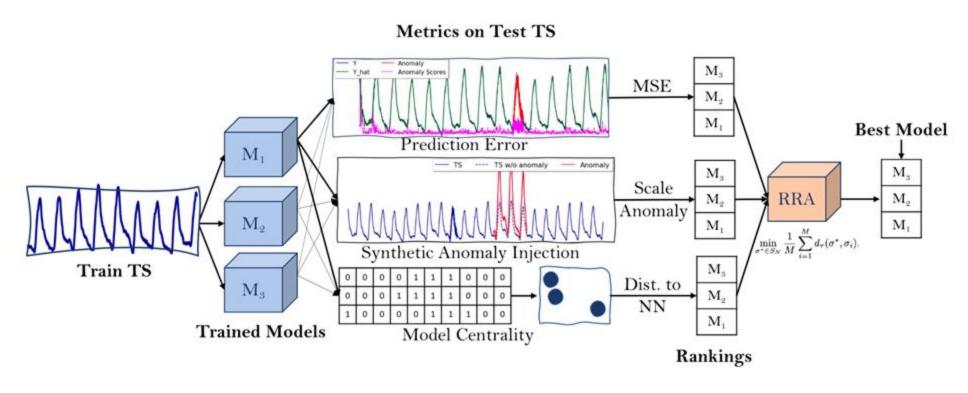
- Stand-alone: Clustering Quality, EM&MV, Synthetic anomaly injection
- Collective: Model Centrality, Rank Aggregation









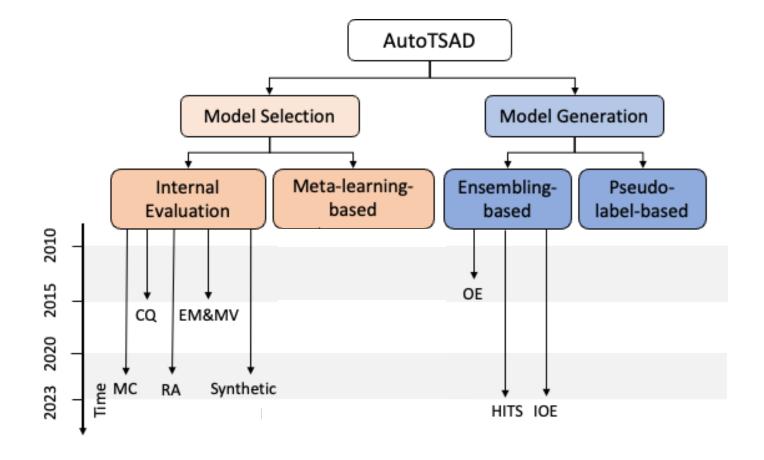


Automated Solution: Ensembling-based

Definition: Integrate predictions from the candidate model set

- Full: OE

- Selective: HITS, IOE

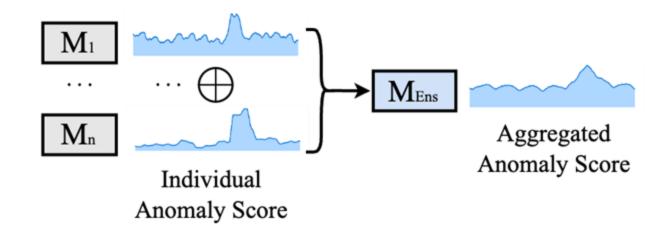


Automated Solution: Ensembling-based

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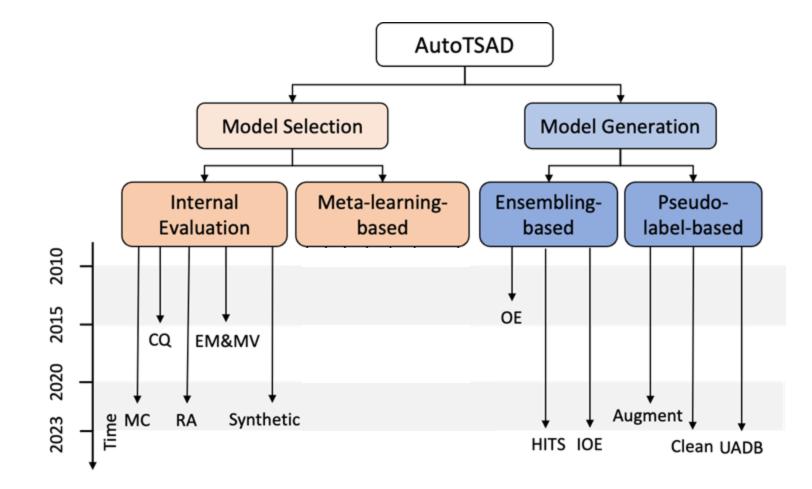


Automated Solution: Pseudo-label-based

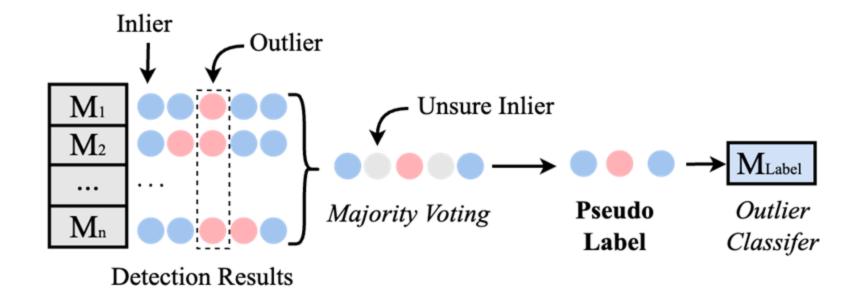
Definition: Generate pseudo-labels to transform the unsupervised anomaly detection problem into a supervised framework

AutoOD: Augment, Clean

- Booster: UADB



Automated Solution: Pseudo-label-based



Pseudo-label-based Method Framework [16].

Automated Solution: Meta-learning-based

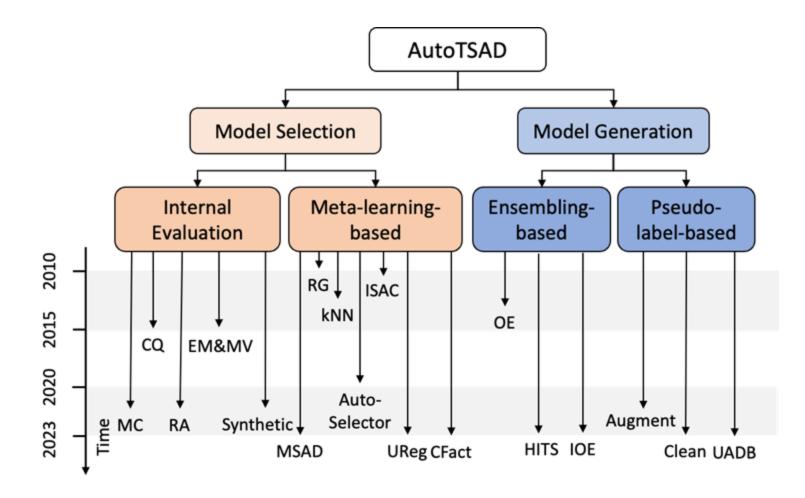
Definition: Using insights from historical labeled datasets to select the best model for new data

Classification: Auto-Selector, MSAD

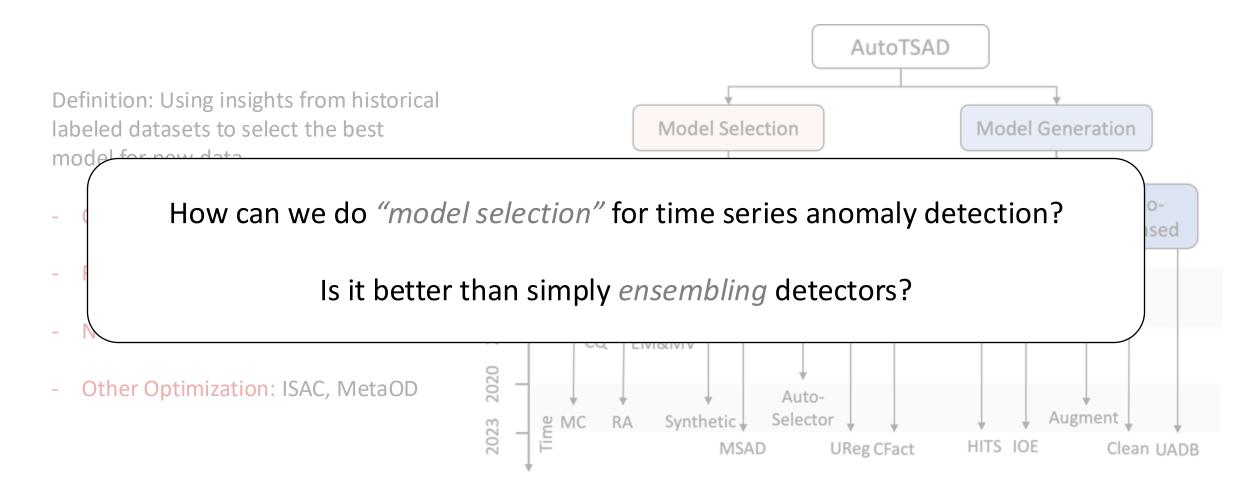
- Regression: RG, UReg, Cfact

Nearest Neighbor: kNN

Other Optimization: ISAC, MetaOD



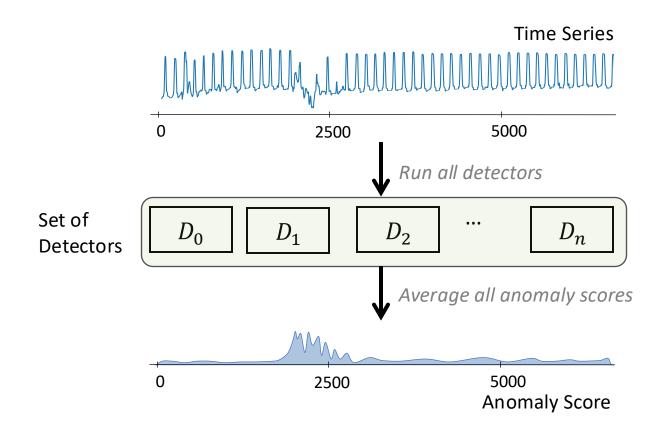
Automated Solution: Meta-learning-based



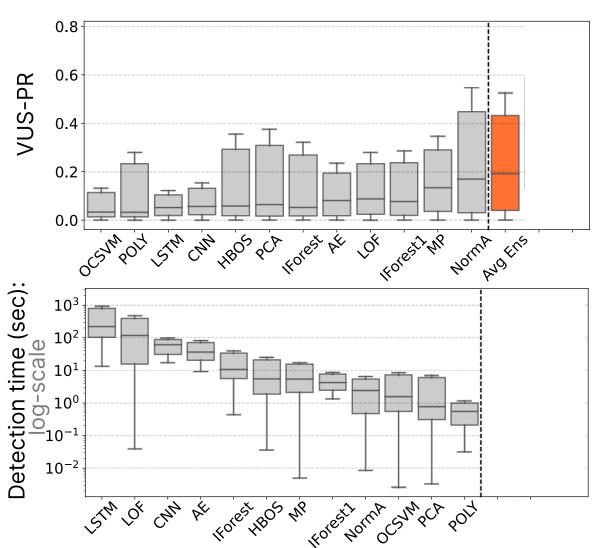
IV. MSAD

Model Selection for Anomaly Detection

Ensembling is proposed as a mitigation strategy to the previous limitation [17]

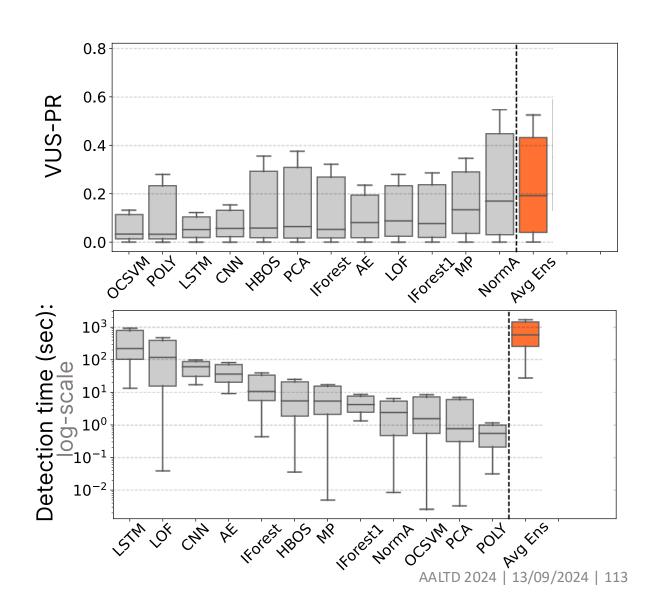


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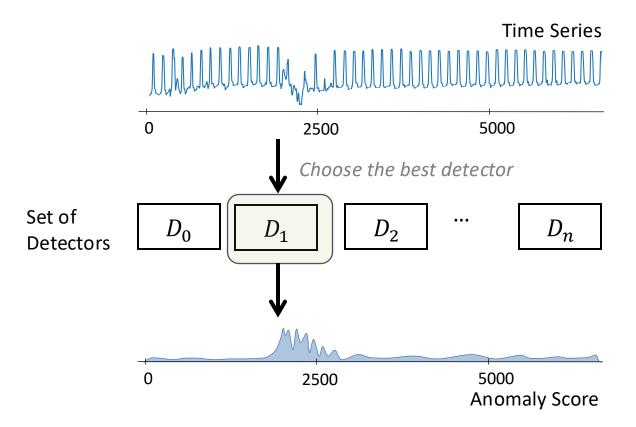
... But is problematic in terms of execution time



Ensembling is proposed as a mitigation strategy to the previous limitation [17]

... But is problematic in terms of execution time

Model Selection (MS) is a solution to reduce the execution time

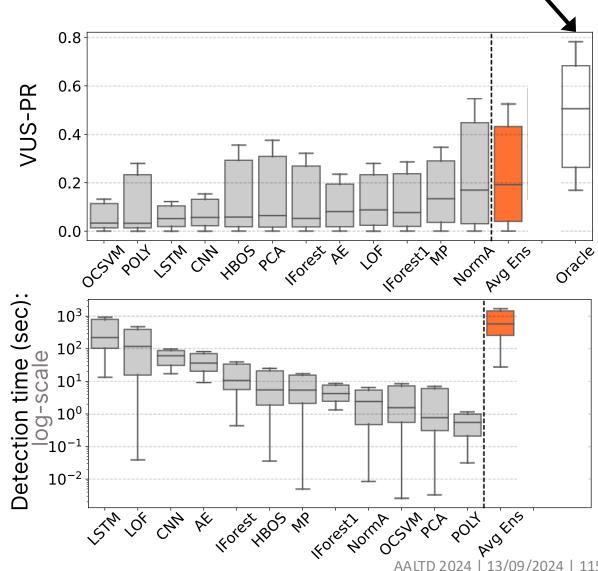


Ensembling is proposed as a mitigation strategy to the previous limitation [17]

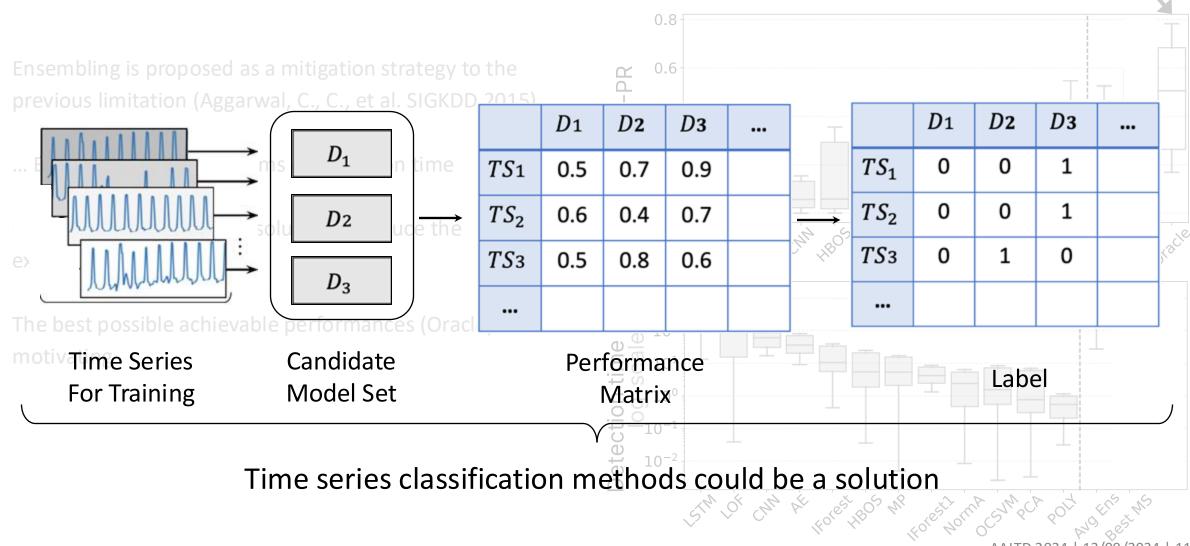
... But is problematic in terms of execution time

Model Selection (MS) is a solution to reduce the execution time

The best possible achievable performances (Oracle) is motivating



Oracle



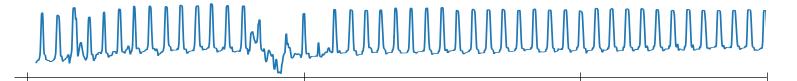
Oracle

MSAD: Classification for Model Selection

Research Questions (RQs)

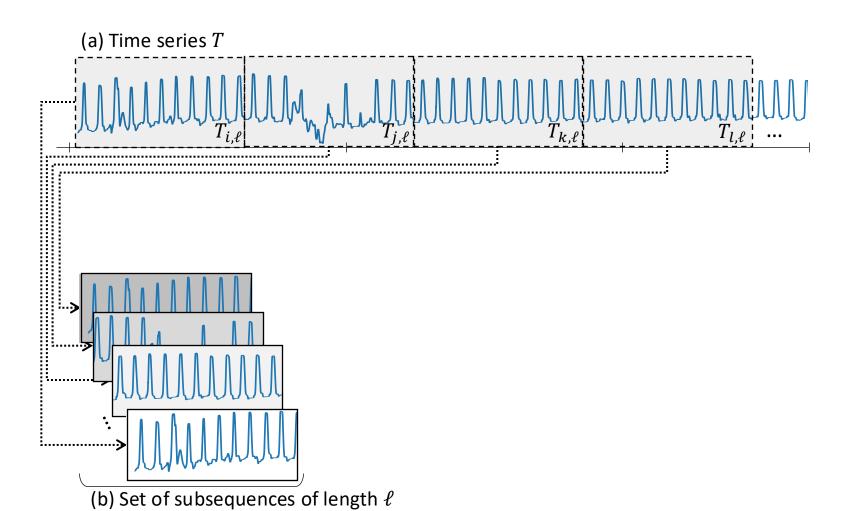
- 1. What is the best approach:
 - 1. Individual Detectors
 - 2. Average Ensembling (Avg Ens)
 - 3. Model Selection (MS)
- 2. What is the best input: Time Series Features OR Raw Values?
- 3. What-if model selection is tested on completely new datasets?

(a) Time series T



Step 1: Acquiring Labeled Time Series

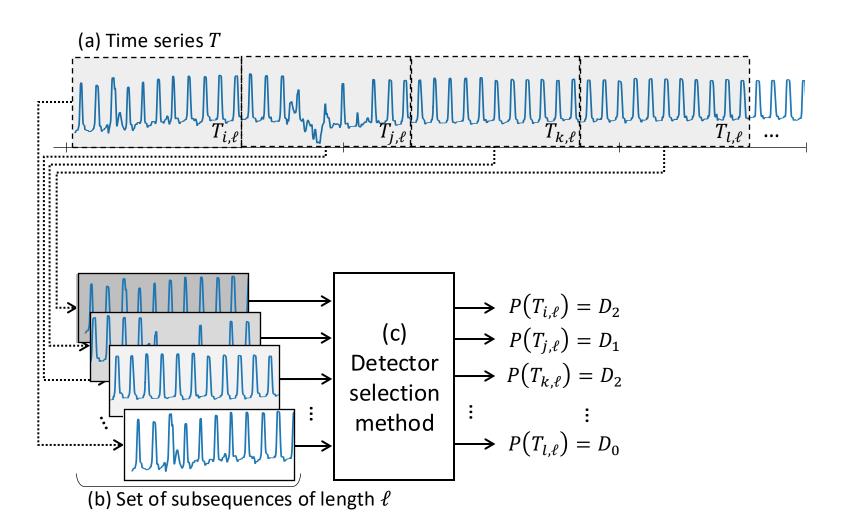
We use the TSB-UAD benchmark [14], on which we know in advance which detector is the best for each time series.



Step 2: Segmentation

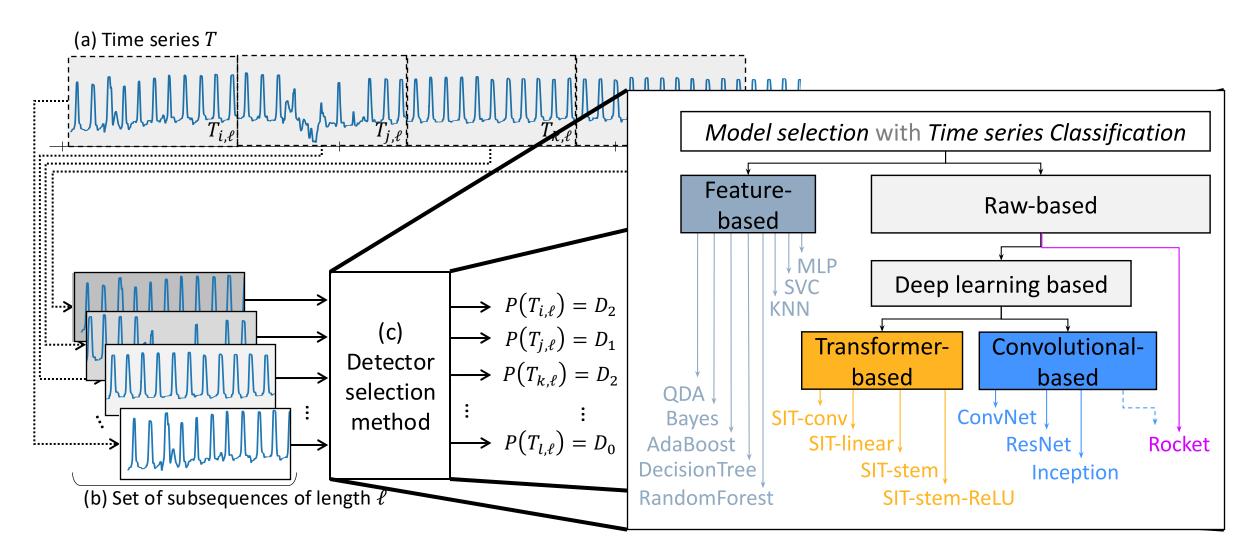
We segment the time series into equal length subsequences.

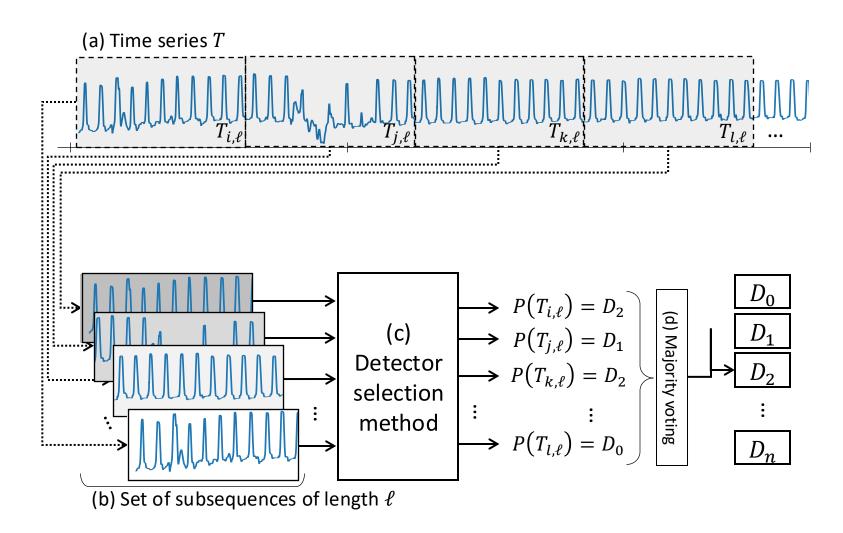
Each subsequence is assigned to the same label (best detector)



Step 3: Prediction

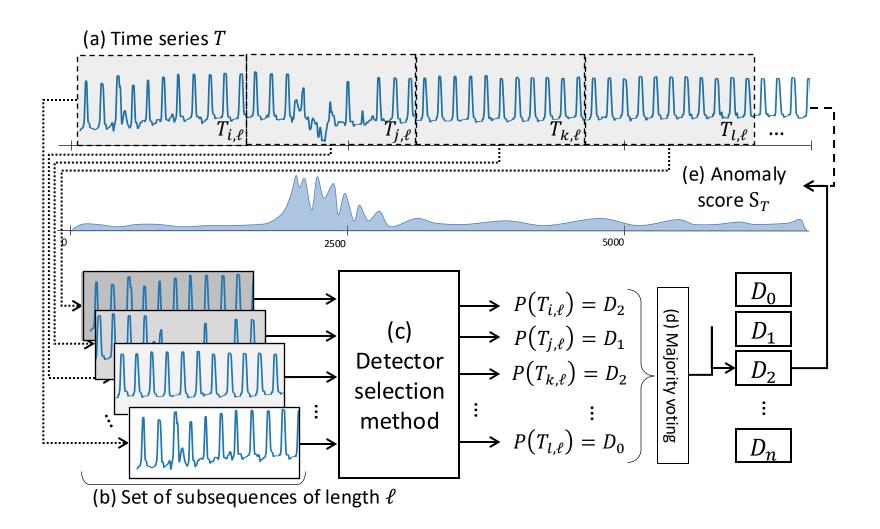
We train a time series classification method to predict which detector is the best (using the labels from TSB-UAD).





Step 4: Selection

We pick the most selected detector for all the subsequences of a time series.



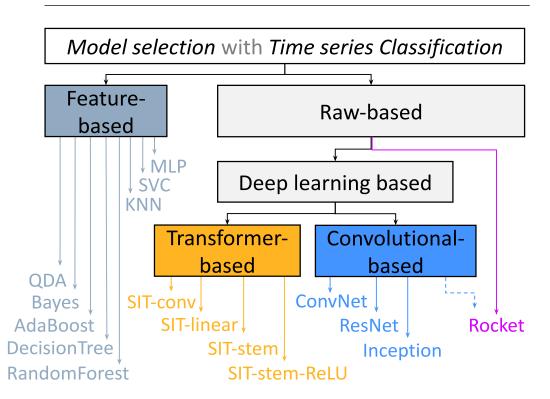
Step 5: Anomaly Score Computation

We finally compute the anomaly score using the selected detector.

We conduct our experimental evaluation on the TSB-UAD benchmark:

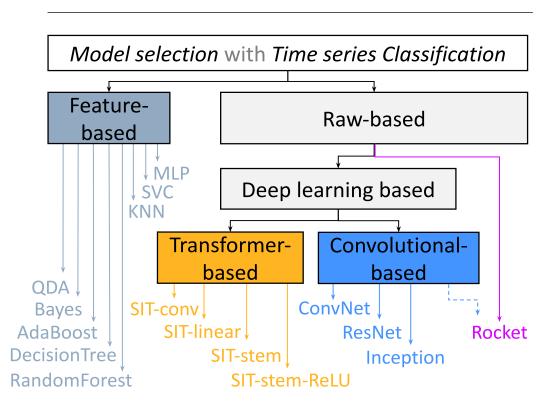
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16 time series classification methods:

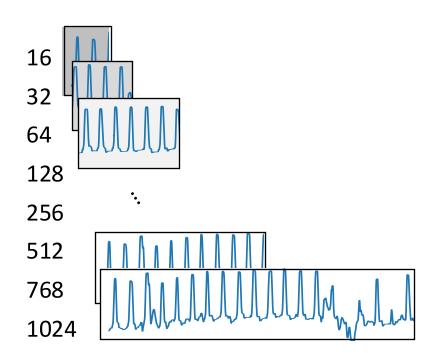


We conduct our experimental evaluation on the TSB-UAD benchmark:

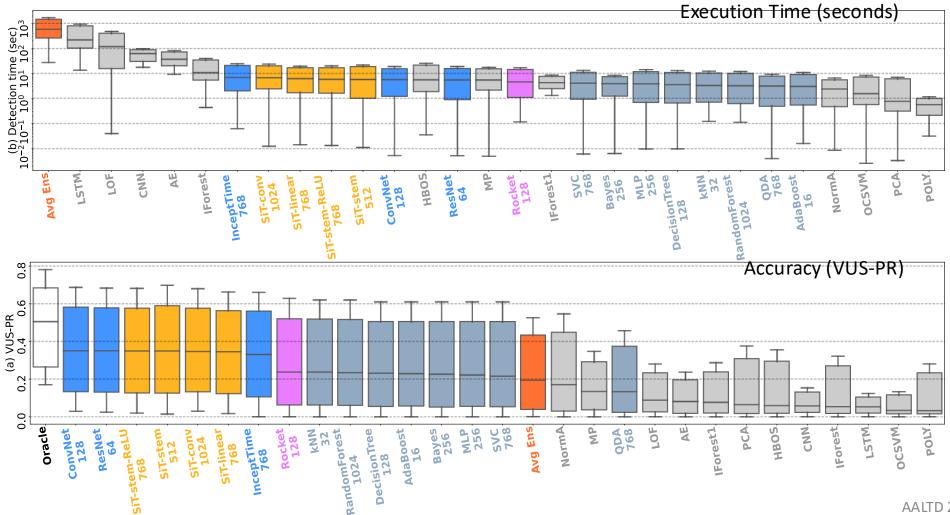
16 time series classification methods:



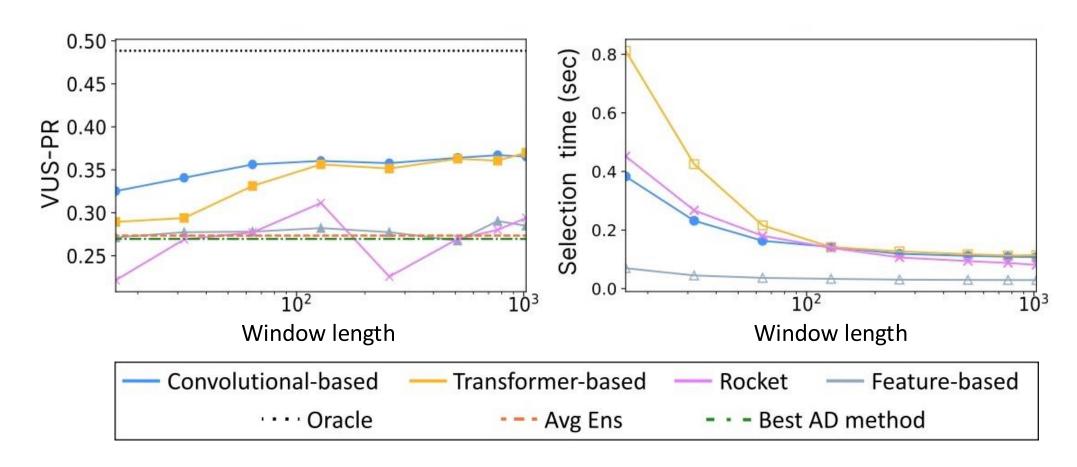
With 8 segmentation window lengths:



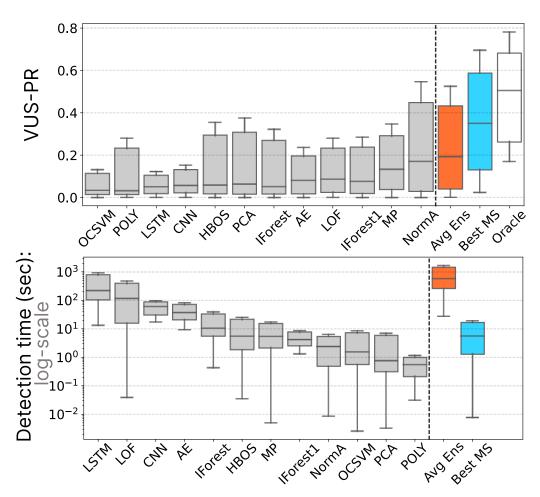
Raw values is the best input compared to time series features



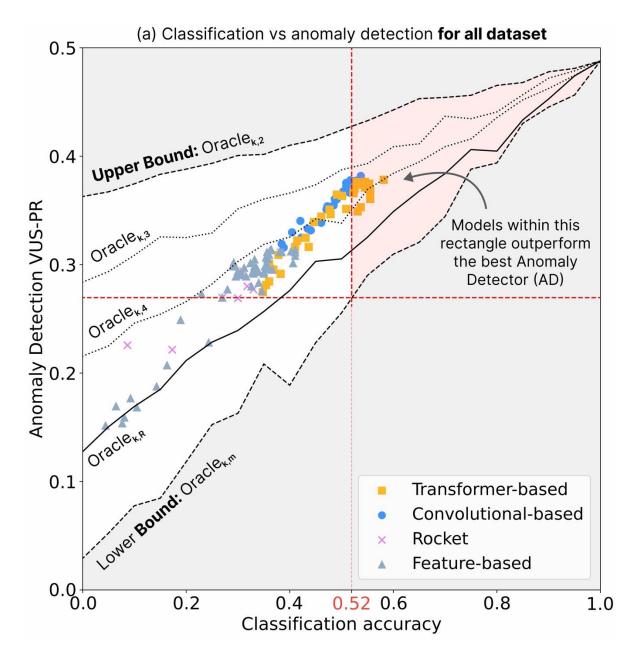
The window length influence is different based on the type of methods



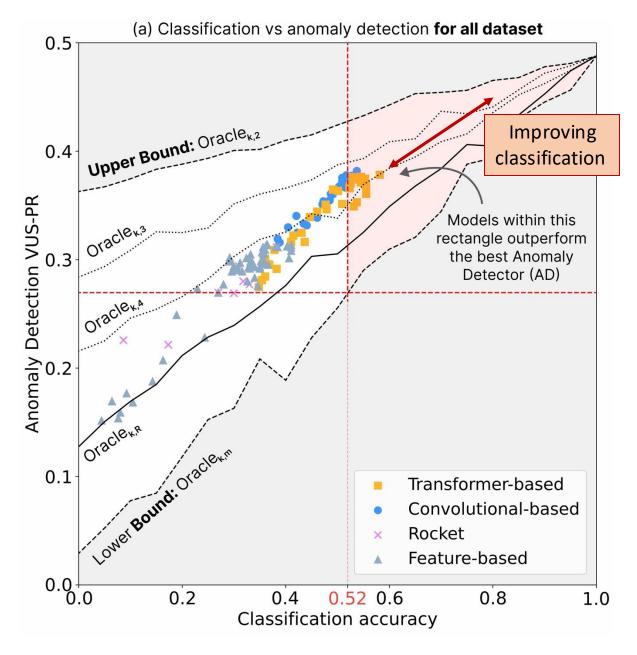
- MS outperforms the Individual detectors and the Avg Ens in terms of accuracy
- MS outperforms Avg Ens in terms of execution time



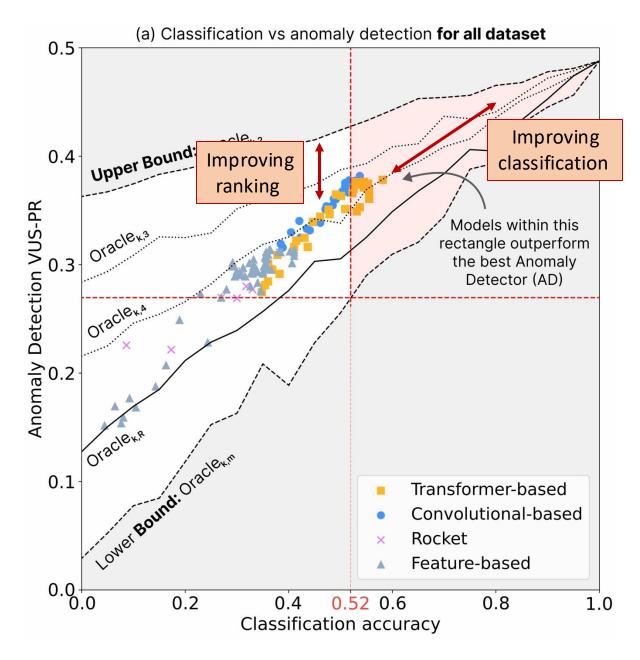
- MS outperforms the Individual detectors and the Avg Ens in terms of accuracy
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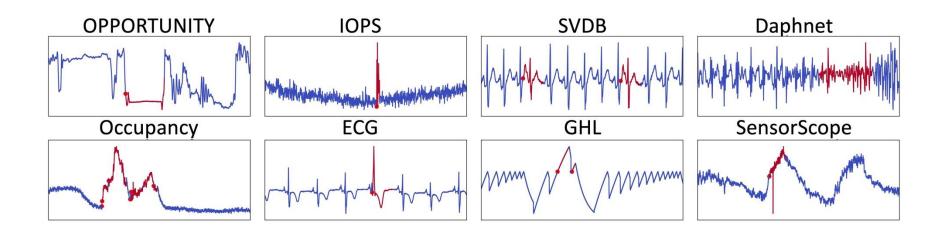


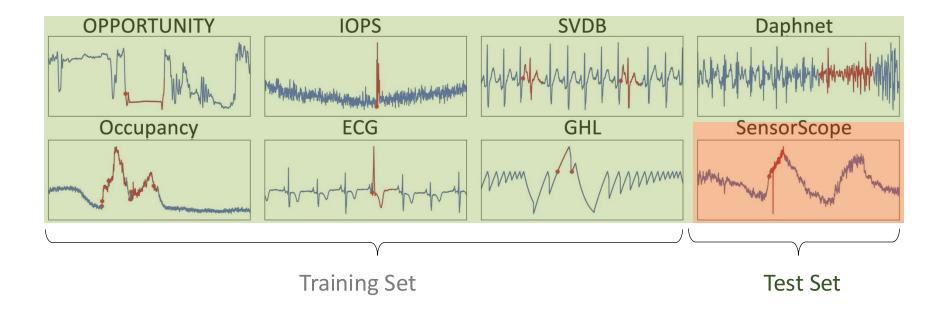
- MS outperforms the Individual detectors and the Avg Ens in terms of accuracy
- MS outperforms Avg Ens in terms of execution time
- Potential improvement in terms of classification



- MS outperforms the Individual detectors and the Avg Ens in terms of accuracy
- MS outperforms Avg Ens in terms of execution time
- Potential improvement in terms of classification
- Potential improvement in terms of ranking detectors



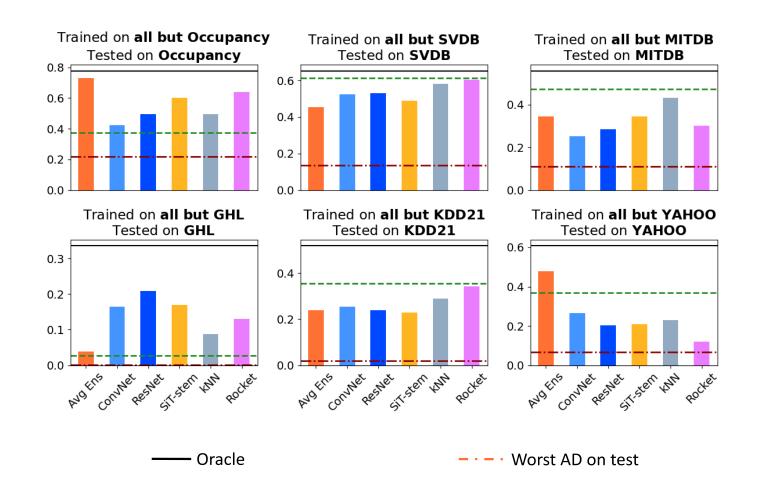






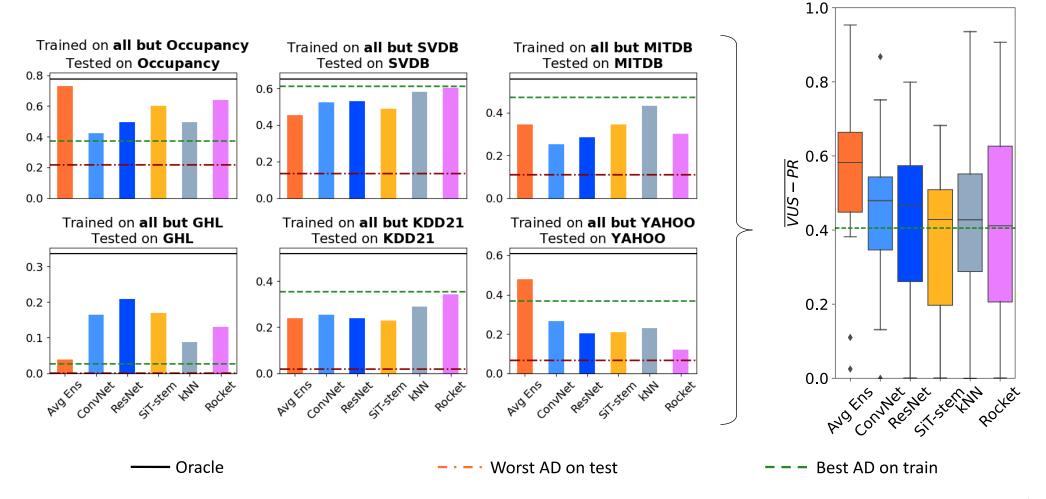
Training Set

Out-of-distribution testing: How well a model handles unfamiliar data?

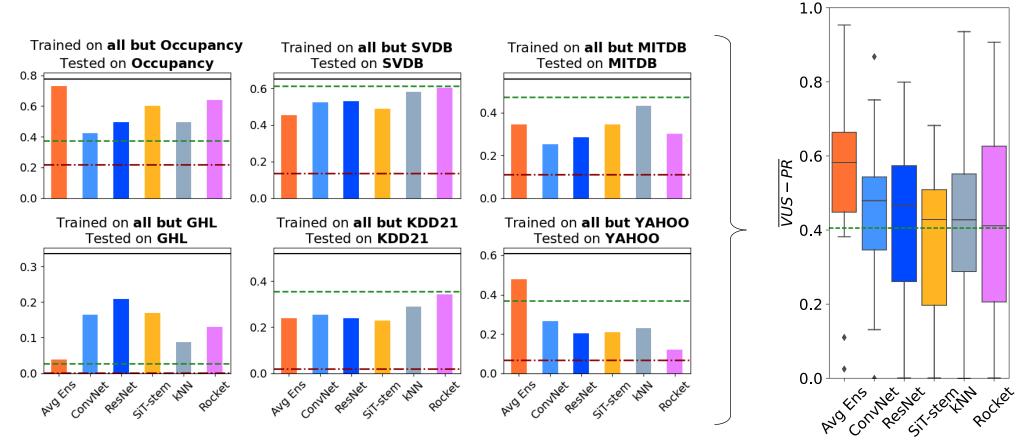


Best AD on train

Out-of-distribution testing: How well a model handles unfamiliar data? (a) Avg VUS-PR for all dataset



Out-of-distribution testing: How well a model handles unfamiliar data? (a) Avg VUS-PR for all dataset



Avg Ens is generally safer in terms of accuracy for new datasets

Out-of

Choose Wisely:

An Extensive Evaluation of Model Selection for Anomaly Detection in Time Series. Emmanouil Sylligardos, Paul Boniol, John Paparrizos, Panos Trahanias, and Themis Palpanas.



Paper (VLDB 2023)



https://helios2.mi.parisdescartes.fr/~themisp/publications/pvldb23-msad.pdf



Demo (ICDE 2024)



https://adecimots.streamlit.app/



GitHub Repo



boniolp/MSAD

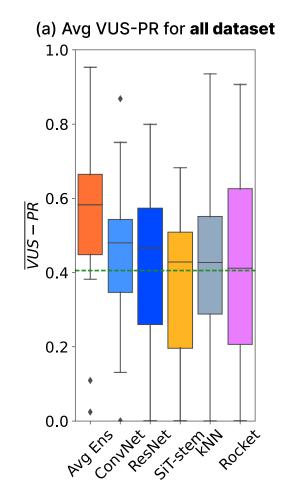


aset

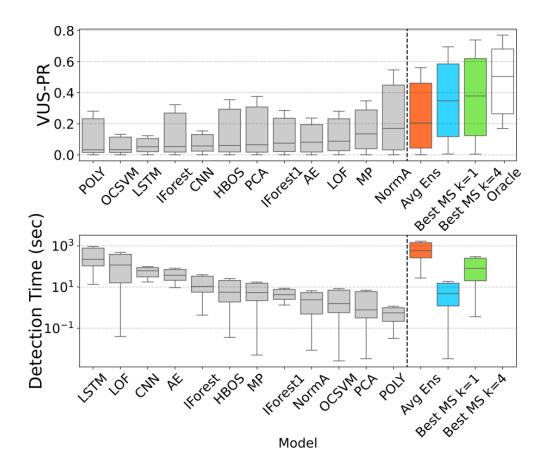
V. Conclusion

Research Directions

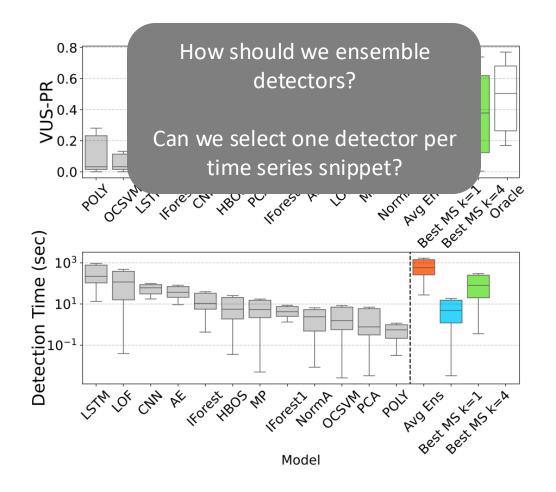
Ensembling is still better for out-of-distribution cases



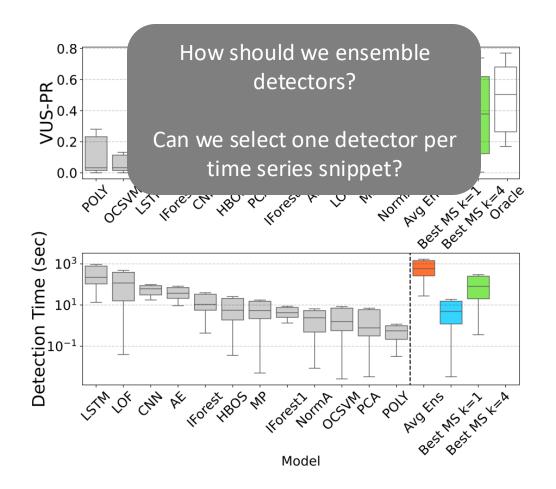
- Ensembling is still better for out-of-distribution cases
 - **Combining Model Selection and Ensembling**



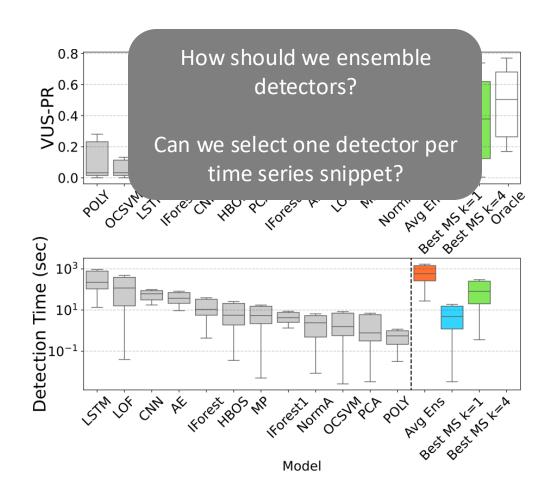
- Ensembling is still better for out-of-distribution cases
 - **Combining Model Selection and Ensembling**



- Ensembling is still better for out-of-distribution cases
 - **Combining Model Selection and Ensembling**
- Ensembling has a strong impact on execution time

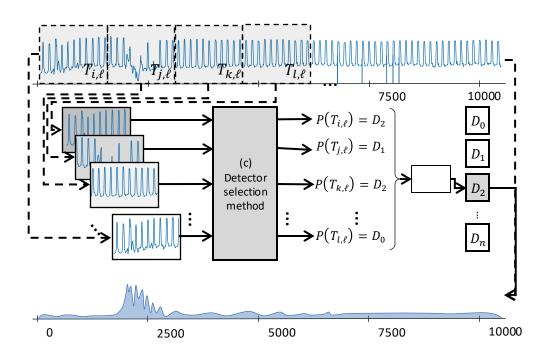


- Ensembling is still better for out-of-distribution cases
 - Combining Model Selection and Ensembling
- Ensembling has a strong impact on execution time
 - Trade-off between execution time and accuracy in the selection process



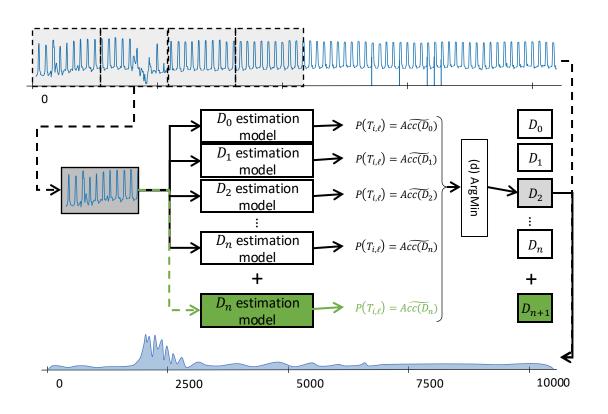
- Ensembling is still better for out-of-distribution cases
 - Combining Model Selection and Ensembling
- Ensembling has a strong impact on execution time
 - Trade-off between execution time and accuracy in the selection process
- Adding a new detector require training from scratch the pipeline

Classification-based



- Ensembling is still better for out-of-distribution cases
 - Combining Model Selection and Ensembling
- Ensembling has a strong impact on execution time
 - Trade-off between execution time and accuracy in the selection process
- Adding a new detector require training from scratch the pipeline
 - Improving modularity (regression-based model selection)

Regression-based



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ICS-FORTH



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Thank you for attending!